

# Link Prediction on Latent Heterogeneous Graphs

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# Outline

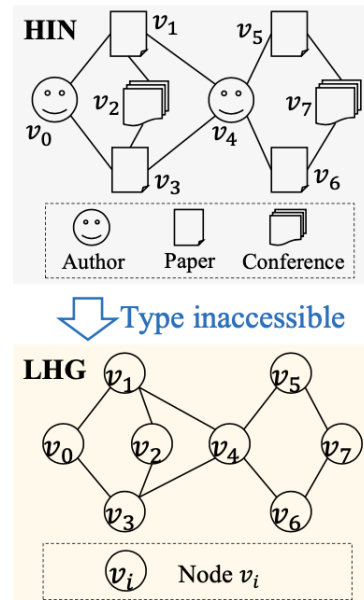
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- **Problem & related work**
- Proposed model: LHGNN
- Experiments
- Conclusions

# Motivation

- **Link prediction:** fundamental task on graph with many applications
- **Heterogeneous Graphs** (or Heterogeneous Information Networks/HIN) consist of multiple types of nodes/edges, providing rich and diverse semantics for link prediction.
- In real-world scenarios, type information of HINs can be noisy, missing or completely inaccessible.

→ **Latent Heterogeneous Graphs (LHG)**



(a) HIN vs. LHG

# Related Work

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- Graph Neural Networks
  - Homogeneous graphs: GCN [1], GAT [2], etc.
  - Heterogeneous graphs: HAT [3], HGT [4], etc.
- Knowledge Graph Embedding
  - TransE [5], TransR [6], etc.
- Predicting Missing Types
  - RPGNN [7], Linear.Adagrad [8], etc.

[1] Kipf, T. N., et al. 2017. Semi-supervised classification with graph convolutional networks. ICLR.

[2] Veličković, P., et al. 2018. Graph attention networks. ICLR.

[3] Wang, et al. 2019. Heterogeneous graph attention network. WWW.

[4] Hu et al. 2020. Heterogeneous graph transformer. WWW.

[5] Bordes et al. 2013. Translating embeddings for modeling multi-relational data. NeurIPS.

[6] Lin et al. 2015. Learning entity and relation embeddings for knowledge graph completion. AAAI.

[7] Zhang et al. 2021. Relation prediction via graph neural network in heterogeneous information networks with missing type information. CIKM.

[8] Neelakantan et al. 2015. Inferring missing entity type instances for knowledge base completion: New dataset and methods. NAACL.

# Problem formulation

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**Latent Heterogeneous Graph (LHG):**  $(V, E, A, R, \psi, \phi)$

- $V, E$ : set of nodes, edges
- $A, R$ : set of node types, and edge types, respectively
- $\psi: V \rightarrow A, \phi: E \rightarrow R$ : type mapping functions
- $A, R, \psi, \phi$ : inaccessible/unknown, yet still exist

**Link Prediction on LHG:** Given a query node, we rank other nodes by their probability of forming a link with the query.

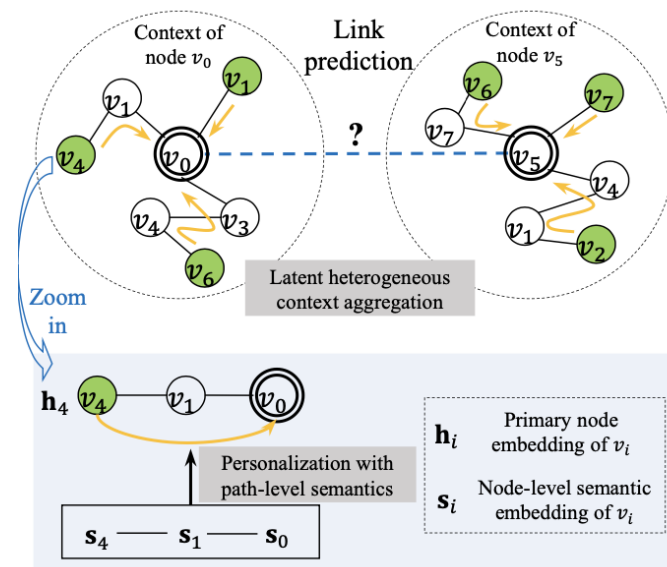
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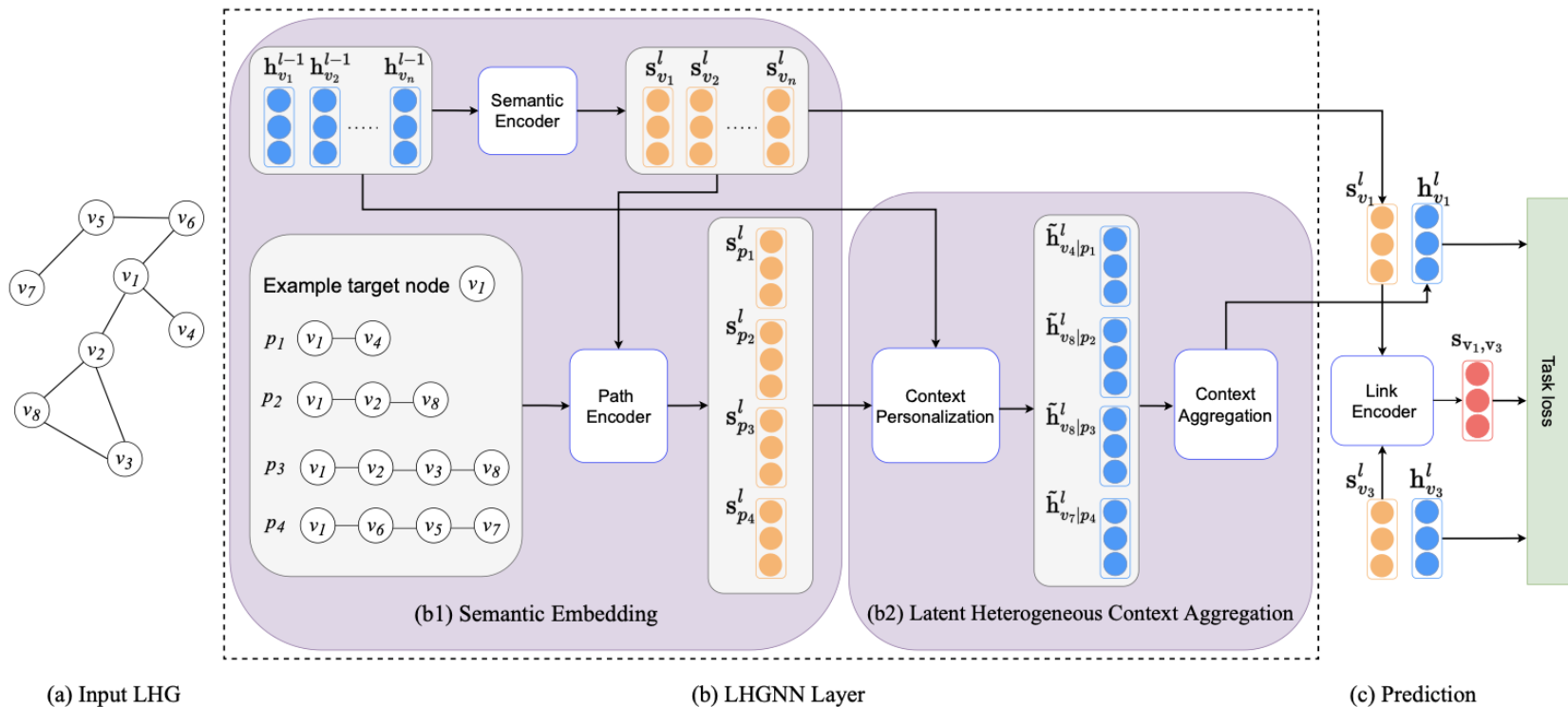
# Challenges

1. How to capture the **latent semantics** on and between nodes without any type information?
2. As contextual nodes of a target node often carry **latent heterogeneous semantics**, how to **differentiate** them for finer-grained context aggregation?



(b) Link prediction on LHG with LHGNN

# LHGNN: Overall Framework





# Semantic Embedding

- Node-level Semantic Embedding

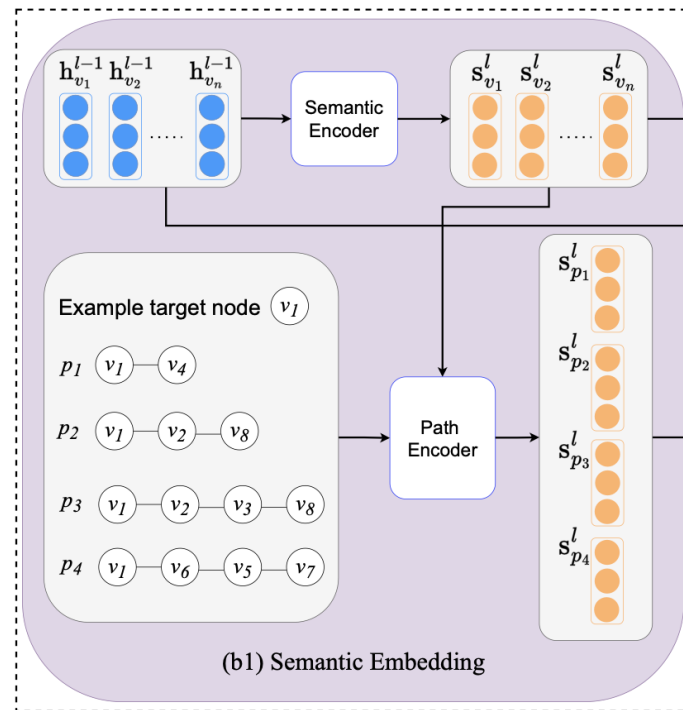
Extracts abstract semantic information from primary node embedding

$$\mathbf{s}_v^l = \text{LEAKYRELU}(\mathbf{W}_s^l \mathbf{h}_v^{l-1} + \mathbf{b}_s^l)$$

- Path-level Semantic Embedding

Captures latent heterogeneous semantics from different context nodes for target node

$$\mathbf{s}_{p_{\langle v, u \rangle}}^l = f_p(\{\mathbf{s}_{v_i}^l \mid v_i \text{ in the path } p_{\langle v, u \rangle}\}):$$



# Latent Heterogeneous Context Aggregation

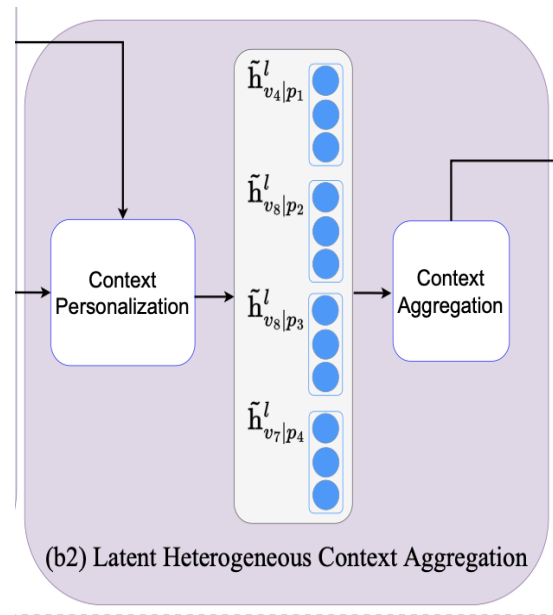
- Context Personalization

Modulates latent heterogeneous semantics from different context nodes

$$\tilde{\mathbf{h}}_{u|p\langle v,u \rangle}^l = (\gamma_{p\langle v,u \rangle}^l + \mathbf{1}) \odot \mathbf{h}_u^{l-1} + \beta_{p\langle v,u \rangle}^l$$

$$\gamma_{p\langle u,v \rangle}^l = \text{LEAKYRELU}(\mathbf{W}_{\gamma}^l \mathbf{s}_{p\langle u,v \rangle}^l + \mathbf{b}_{\gamma}^l)$$

$$\beta_{p\langle u,v \rangle}^l = \text{LEAKYRELU}(\mathbf{W}_{\beta}^l \mathbf{s}_{p\langle u,v \rangle}^l + \mathbf{b}_{\beta}^l)$$



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# Experimental setup

## Datasets

Attributes	FB15k-237	WN18RR	DBLP	OGB-MAG
# Nodes	14,541	40,943	18,405	100,002
# Edges	310,116	93,003	67,946	1,862,256
# Features	-	-	334	128
# Relations	237	11	4	4
Avg(degree)	29.09	3.50	3.55	17.88
# Training	272,115	86,835	54,356	1,489,804
# Validation	17,535	3,034	6,794	186,225
# Testing	20,466	3,134	6796	186,227

## Baselines

- GNN:  
GCN [1], GAT [2], SAGE [3]
- Translation:  
TransE [4], TransR [5]
- HGNN:  
HAN [6], HGT [7], HGN [8]

## Metrics

- MAP, NDCG

[1] Kipf, T. N., et al. 2017. Semi-supervised classification with graph convolutional networks. ICLR.

[2] Veličković, P., et al. 2018. Graph attention networks. ICLR.

[3] Hamilton W L., et al. 2017. Inductive representation learning on large graphs. NeurIPS.

[4] Bordes et al. 2013. Translating embeddings for modeling multi-relational data. NeurIPS.

[5] Lin et al. 2015. Learning entity and relation embeddings for knowledge graph completion. AAAI.

[6] Wang, et al. 2019. Heterogeneous graph attention network. WWW.

[7] Hu et al. 2020. Heterogeneous graph transformer. WWW.

[8] Lv et al. 2021. Are we really making much progress? revisiting, benchmarking and refining heterogeneous graph neural networks. KDD.

# Link Prediction

**Table 2: Evaluation of link prediction on LHGs. Best is bolded and runner-up underlined; OOM means out-of-memory error.**

Methods	FB15k-237		WN18RR		DBLP		OGB-MAG	
	MAP	NDCG	MAP	NDCG	MAP	NDCG	MAP	NDCG
GCN	0.790 ± 0.001	0.842 ± 0.001	0.729 ± 0.002	0.794 ± 0.001	0.879 ± 0.001	0.910 ± 0.001	0.848 ± 0.001	0.886 ± 0.001
GAT	0.786 ± 0.002	0.839 ± 0.001	0.761 ± 0.001	0.818 ± 0.001	<u>0.913</u> ± 0.001	<u>0.936</u> ± 0.001	0.830 ± 0.004	0.872 ± 0.003
GraphSAGE	<u>0.800</u> ± 0.001	<u>0.850</u> ± 0.001	0.728 ± 0.003	0.793 ± 0.002	0.891 ± 0.001	0.918 ± 0.001	<u>0.849</u> ± 0.001	<u>0.887</u> ± 0.001
TransE	0.675 ± 0.001	0.752 ± 0.001	0.511 ± 0.002	0.624 ± 0.001	0.488 ± 0.001	0.605 ± 0.001	0.552 ± 0.001	0.656 ± 0.001
TransR	0.734 ± 0.004	0.798 ± 0.003	0.510 ± 0.002	0.623 ± 0.001	0.565 ± 0.007	0.668 ± 0.005	0.546 ± 0.001	0.652 ± 0.001
HAN	0.725 ± 0.002	0.793 ± 0.002	0.749 ± 0.003	0.810 ± 0.003	0.763 ± 0.005	0.801 ± 0.004	OOM	OOM
HGT	0.782 ± 0.001	0.837 ± 0.001	0.724 ± 0.003	0.791 ± 0.002	0.897 ± 0.001	0.923 ± 0.001	0.835 ± 0.003	0.876 ± 0.002
HGN	0.742 ± 0.002	0.806 ± 0.001	<u>0.802</u> ± 0.002	<u>0.849</u> ± 0.002	0.907 ± 0.003	0.930 ± 0.002	0.818 ± 0.001	0.863 ± 0.001
LHGNN	<b>0.858 ± 0.001</b>	<b>0.893 ± 0.001</b>	<b>0.838 ± 0.003</b>	<b>0.877 ± 0.002</b>	<b>0.932 ± 0.003</b>	<b>0.949 ± 0.002</b>	<b>0.879 ± 0.001</b>	<b>0.909 ± 0.001</b>

# Node Type Classification

**Table 5: Evaluation of node type classification on LHGs.**

Methods	DBLP		OGB-MAG	
	MacroF	Accuracy	MacroF	Accuracy
GCN	$0.376 \pm 0.009$	$0.785 \pm 0.002$	$0.599 \pm 0.011$	$0.890 \pm 0.003$
GAT	$0.310 \pm 0.003$	$0.782 \pm 0.001$	$0.624 \pm 0.035$	$0.894 \pm 0.007$
GraphSAGE	<u><math>0.477 \pm 0.021</math></u>	<u><math>0.842 \pm 0.012</math></u>	$0.550 \pm 0.014$	$0.902 \pm 0.004$
HGT	$0.464 \pm 0.009$	$0.837 \pm 0.005$	$0.823 \pm 0.018$	<b><math>0.973 \pm 0.003</math></b>
HGN	$0.292 \pm 0.001$	$0.778 \pm 0.001$	$0.531 \pm 0.003$	$0.847 \pm 0.003$
LHGNN	<b><math>0.662 \pm 0.001</math></b>	<b><math>0.995 \pm 0.001</math></b>	<b><math>0.884 \pm 0.002</math></b>	<u><math>0.953 \pm 0.001</math></u>

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# Conclusions

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- **Problem**
  - Link prediction on Latent Heterogeneous Graph
- **Proposed model: LHGNN**
  - Address the absence of type information
  - Propose the novel idea of **semantic embedding** at both node and path levels to capture latent semantics
  - **Personalize the aggregation** of latent heterogeneous contexts for target nodes in a fine-grained manner
- **Experiments**



# Thanks!



Paper



Code

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