# RoundTripRank

## Graph-based Proximity with Importance and Specificity


| | |
|---|---|
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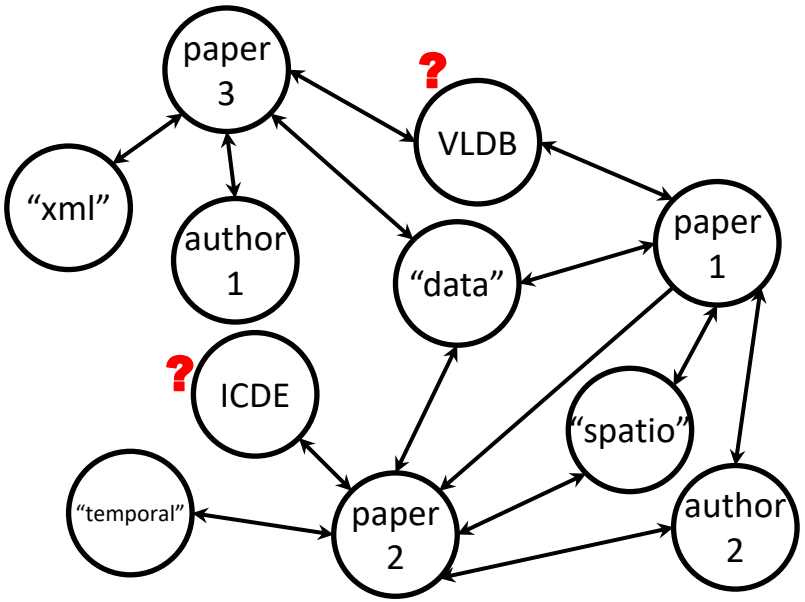
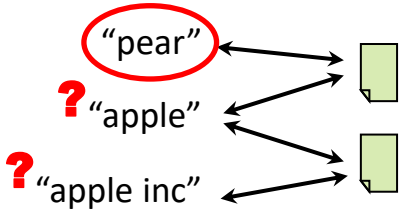
# Graph-based proximity has many applications with different ranking needs

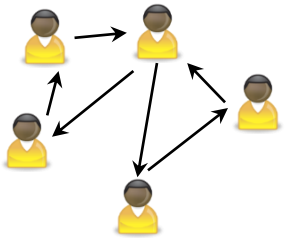
*Citation graph*



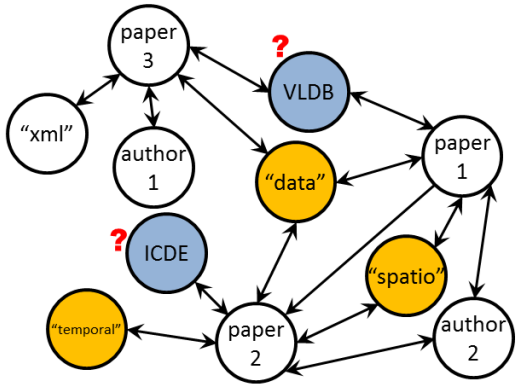

*Query log graph*




*Social network*



# Although various applications involve different needs, ranking by existing graph proximity is limited




**Query**

"spatio", "temporal", "data"

**Matching venues by P-PageRank**

| | |
|---|---|
| SIGMOD | Intl Conference |
| VLDB | Intl Conference |
| ICDE | Intl Conference |

Looks reasonable?
What's missing?

favor very **popular** or **important** venues

only **categorically related** as data topics

**"schema", "matching"**?

# Other venues are needed for different purposes

**Query**

"spatio", "temporal", "data"

**More *specific* venues?**

| | | |
|---|---|---|
| quick background study | Spatio-Temporal Databases | Springer Book |
| report preliminary results | Spatio-Temporal Data Mining | Intl Workshop |
| | Temporal Aspects in Information Systems | Working Conference |

**A *balanced* mixture of venues?**

| | | |
|---|---|---|
| important | VLDB | Intl Conference |
| specific | Spatio-Temporal Databases | Springer Book |
| balanced | ACM SIGSPATIAL/GIS | Intl Conference |

# **Specificity** has been traditionally ignored

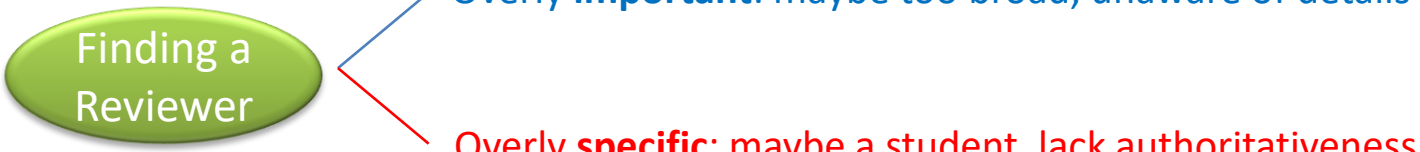
*Semantics*

*Methodology*

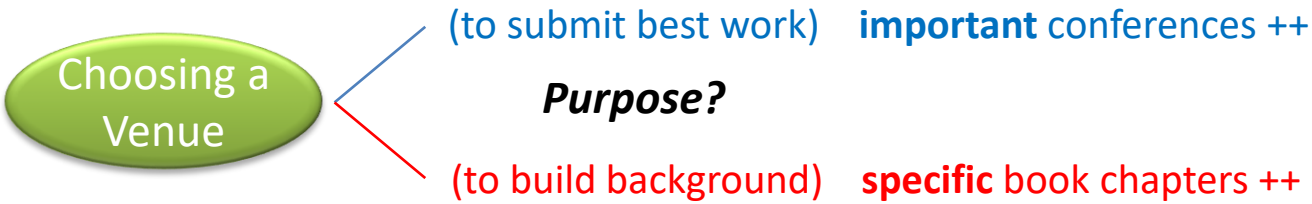
| | Closeness | Importance | Specificity |
|---|---|---|---|
| Common neighbor | Jaccard coefficient [Jaccard1901]<br>AdamicAdar [Adamic2003] | | |
| Hitting time | Escape probability [Koren2006, Tong2007]<br>SimRank [Jeh2002] | | |
| Reachability | | P-PageRank [Page1999]<br>ObjectRank [Balmin2004]<br>PopRank [Nie2005] | |
| Ad-hoc | Katz [Katz1953] | | InvObjectRank<br>Inverse global ObjectRank<br>Inverse node degree [Hristidis2008] |

# Applications require **varying degrees of trade-off** between importance and specificity

**Observation 1**
Most Tasks Require Both Importance and Specificity.




**Observation 2**
The Desirable Trade-off Varies from Task to Task.



# Addressing the two observations is challenging

**Challenge 1:** How do we unify importance & specificity into a single proximity measure?


Generalize random walk based importance to integrate specificity.

**Challenge 2:** How do we generalize our unified model to accommodate flexible trade-offs?

more importance  more specificity

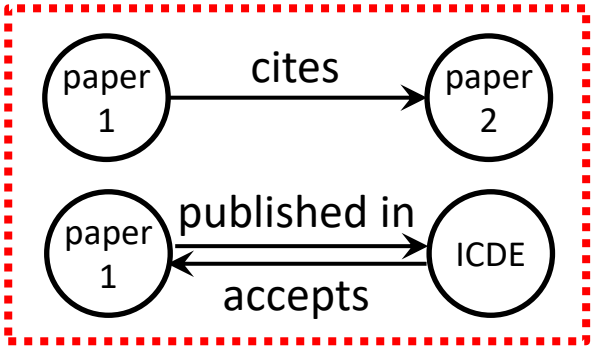
**Challenge 3:** How do we efficiently compute the proximity measure?

Real-time search is indispensable.

**Challenge 1**

How do we *unify importance & specificity* into a single proximity measure?

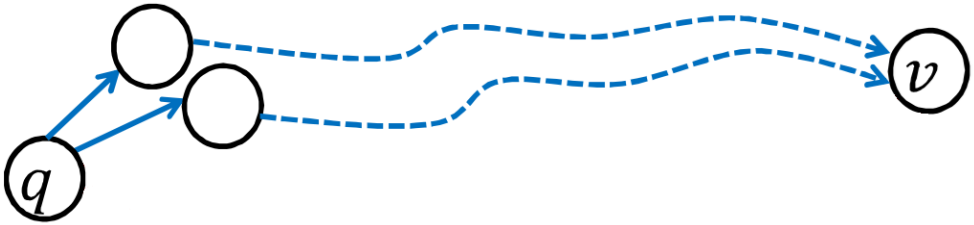
# Let's first review **reachability-based importance** for generalization to specificity




"citations" or "endorsements"

**If node $v$ is important to query $q$…**

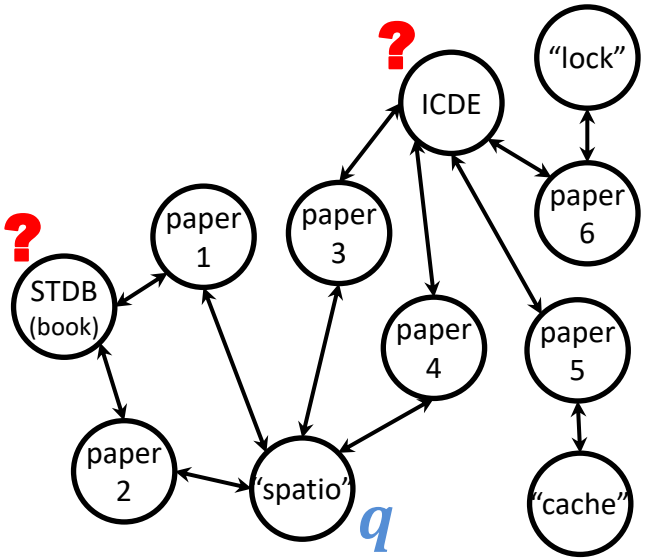
- $q$ is likely to **cite** $v$, directly or indirectly
- Reachability from $q$ to $v$



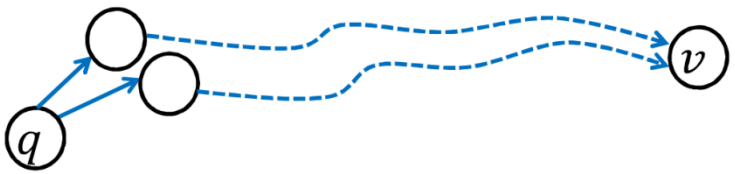
# Generalize importance to specificity
## based on the same citation analogy

**If node $v$ is specific to query $q$…**

- $v$ tends to cite nodes more tailored to $q$
- $q$ is likely to **be cited by** $v$, directly or indirectly
- Reachability from $v$ to $q$




**Importance of $v$ to $q$**

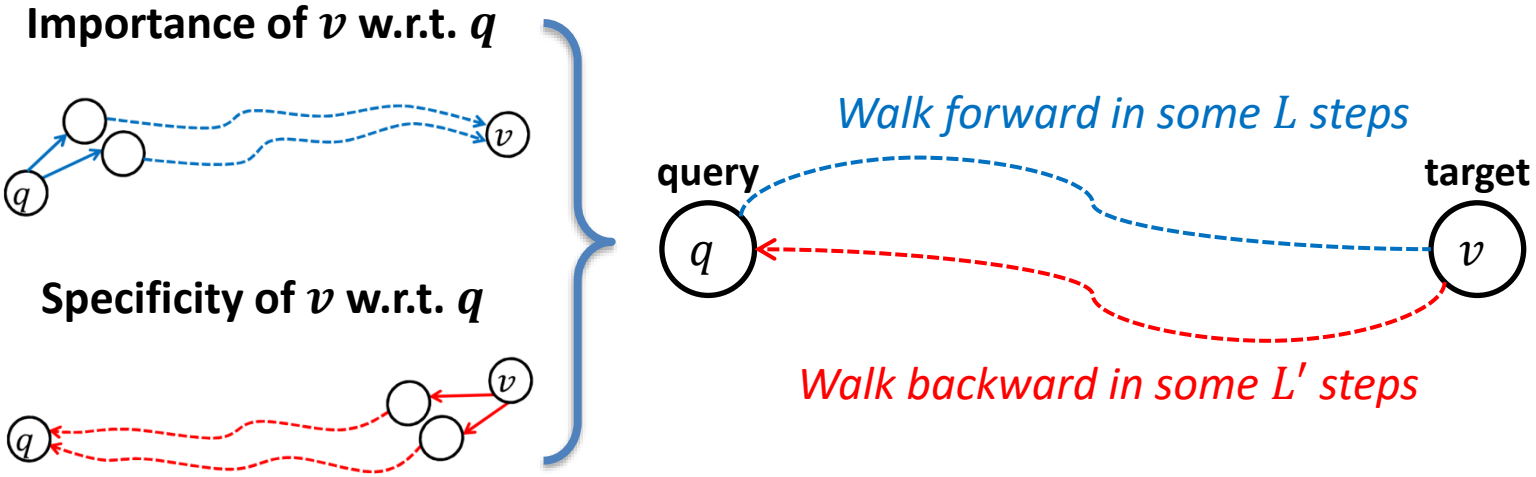



forward walk $q \rightarrow v$

**Specificity of $v$ to $q$**


backward walk $v \rightarrow q$

# Unify forward and backward walks into a **round trip** for both importance & specificity




**Random walk:** $W_0, W_1, \ldots, W_L, W_{L+1}, \ldots, W_{L+L'}$

**Round trip:** $W_0 = W_{L+L'}$

**Target node:** $W_L$

**RoundTripRank:** $r(q,v) \triangleq p(W_L = v | W_0 = W_{L+L'}, W_0 = q)$

## Challenge 2

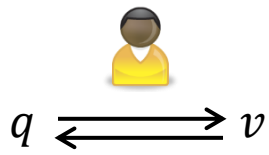
How do we *generalize our unified model* to accommodate flexible trade-offs?

⬇

Based on the same principle of random walk in a round trip.

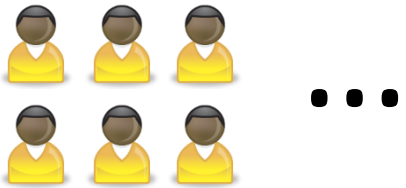
# Further generalize RoundTripRank using **hybrid random surfers** of different goals

Single random surfer $\omega$




Goal: balance b/w importance and specificity

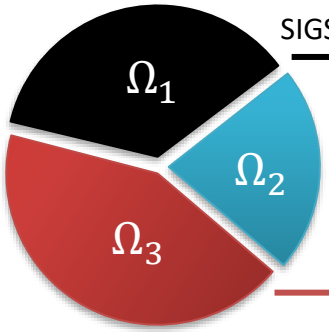
Hybrid random surfer $\Omega$



Different surfers $\omega \in \Omega$ may have different goals!

# Generalize the behaviors of hybrid random surfers for **customizable trade-offs**

**Hybrid Surfers**




SIGSPATIAL/GIS — balance — $q \rightleftarrows v$

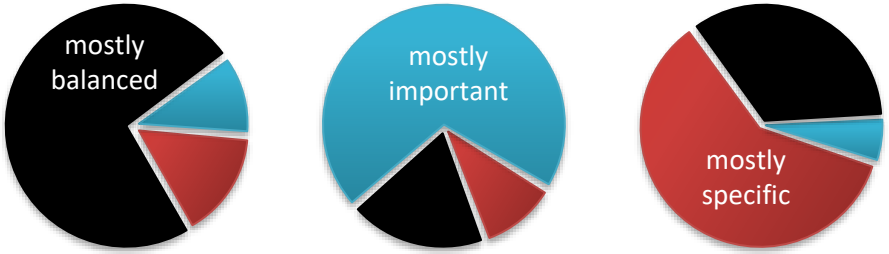
VLDB — importance — $q \rightleftarrows v$

STDB — specificity — $q \rightleftarrows v$

**RoundTripRank+**

$$r_{\Omega}(q,v) \triangleq p(x = v | \forall \omega \in \Omega: W_0^{\omega} = W_{L+L'}^{\omega} = q, W_L^{\omega} = x)$$

**Adjusting Composition**

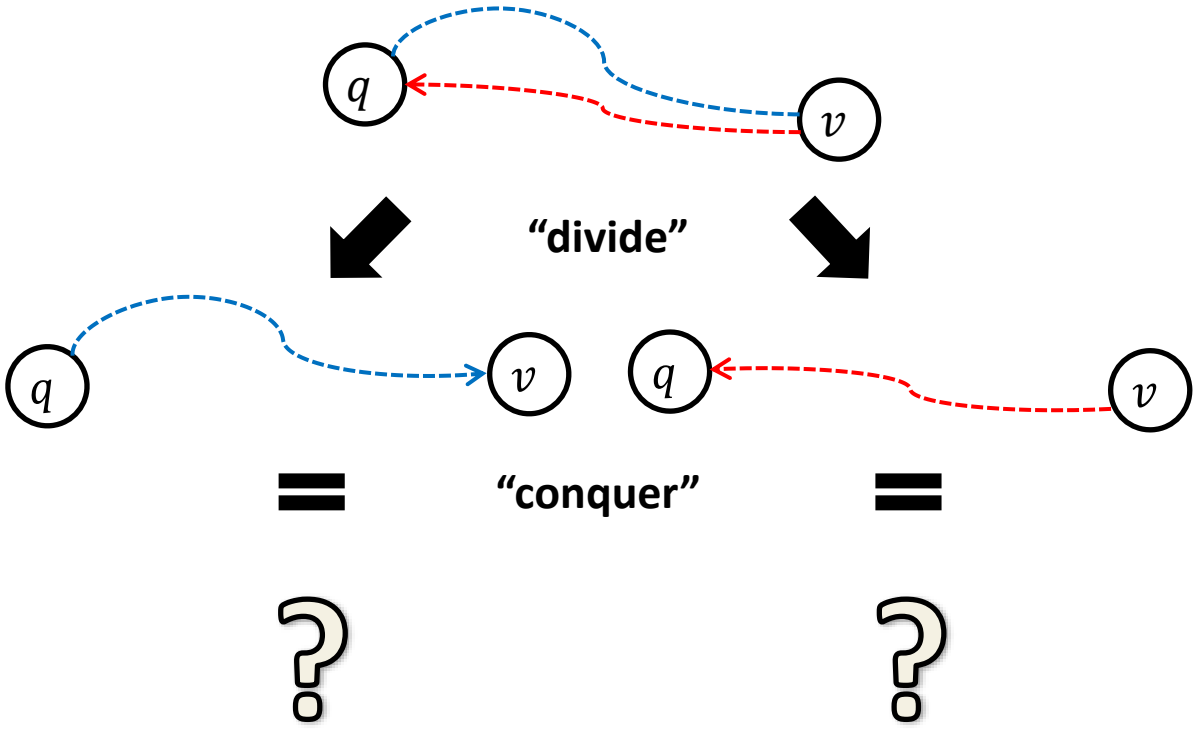



$\rightarrow \beta$

**Challenge 3**

How do we efficiently compute the proximity measure?

# Compute RoundTripRank by "**divide & conquer**"



# Compute RoundTripRank by "**divide & conquer**"

$$r(q,v) \propto$$

**"divide"**

$$p(W_L = v|W_0 = q) \times p(W_{L'} = q|W_0 = v)$$

**"conquer"**

**F-Rank:** $f(q,v)$
(reachability FROM $q$)

**T-Rank:** $t(q,v)$
(reachability TO $q$)

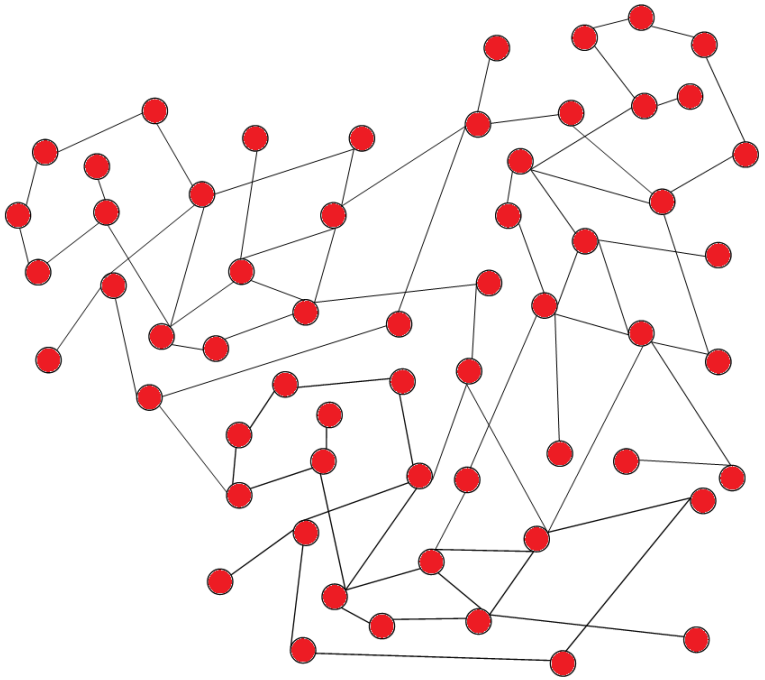
**RoundTripRank**: $r(q,v) \propto f(q,v)t(q,v)$

**RoundTripRank+**: $r_\Omega(q,v) \propto f(q,v)^{1-\beta} t(q,v)^{\beta}$

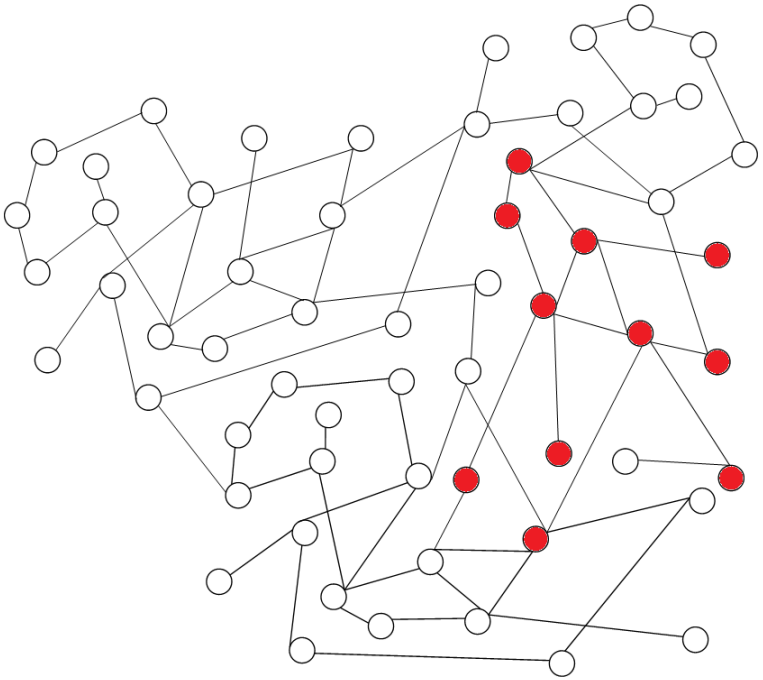
Specificity bias: $\beta = \frac{|\Omega_1|+|\Omega_3|}{2|\Omega_1|+|\Omega_2|+|\Omega_3|} \in [0,1]$

# Top-*K* ranking is more practical & scalable

**Full ranking**
[over the entire graph]

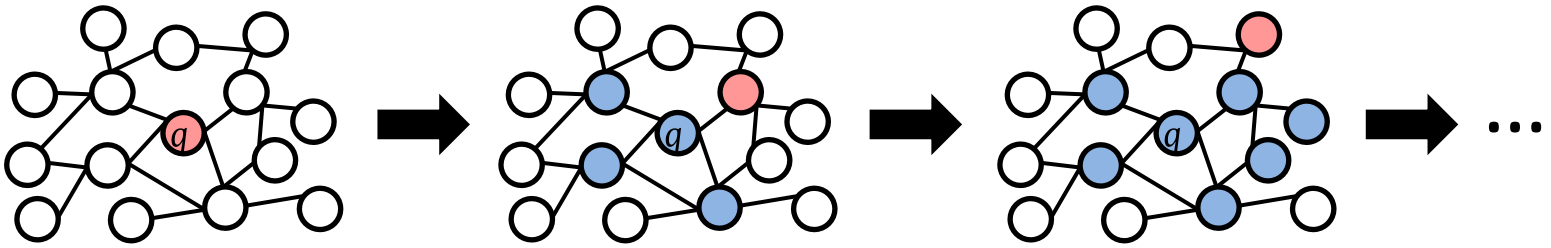


**Top-*K* ranking**
[based on a neighborhood]



# Branch-and-bound algorithm

**Neighborhood expansion**




**Bounds**

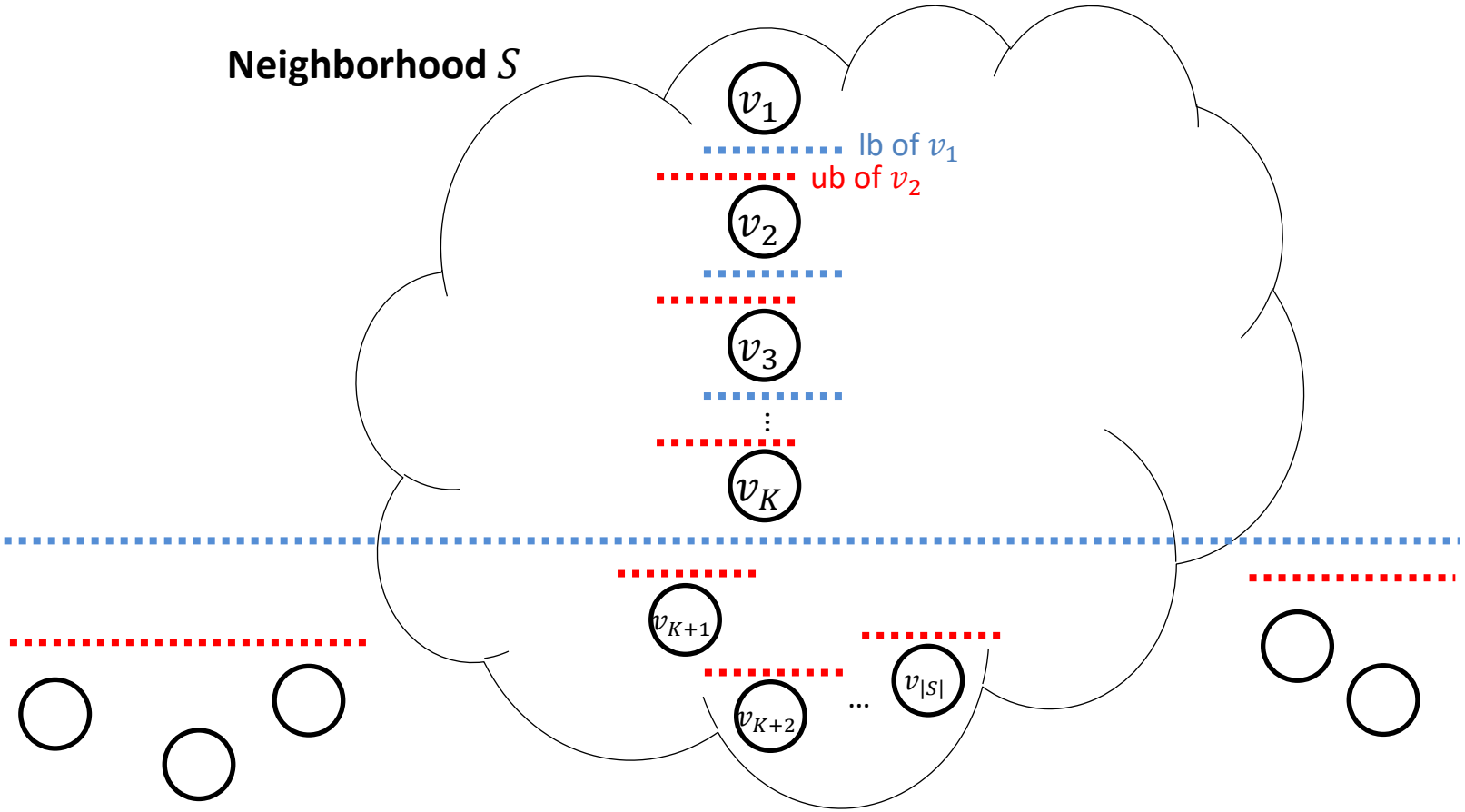
Given the current neighborhood $S$:

$$\check{r}(q,v) \leq r(q,v) \leq \hat{r}(q,v), \forall v \in S$$

$$r(q,v) \leq \hat{r}(q), \forall v \notin S$$

} determine top-$K$ nodes

# Is a candidate top-$K$ ranking $v_1, \ldots, v_K$ correct?




$$\check{r}(q, v_i) > \hat{r}(q, v_{i+1}) - \epsilon \qquad \forall i \in \{1, \ldots, K-1\}$$

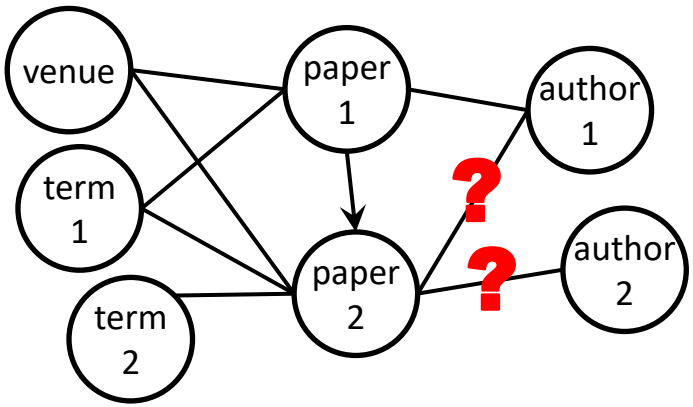
$$\check{r}(q, v_K) > \max\left\{\hat{r}(q, v_{K+1}), \ldots, \hat{r}(q, v_{|S|}), \hat{r}(q)\right\} - \epsilon$$

# Experiments

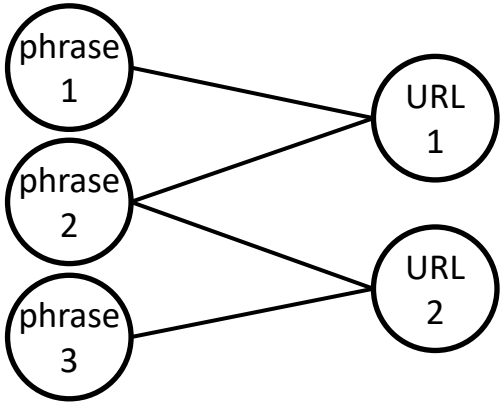
# Experimental Setup

**Graphs**

Bibliographic network (BibNet)




Query log graph (QLog)

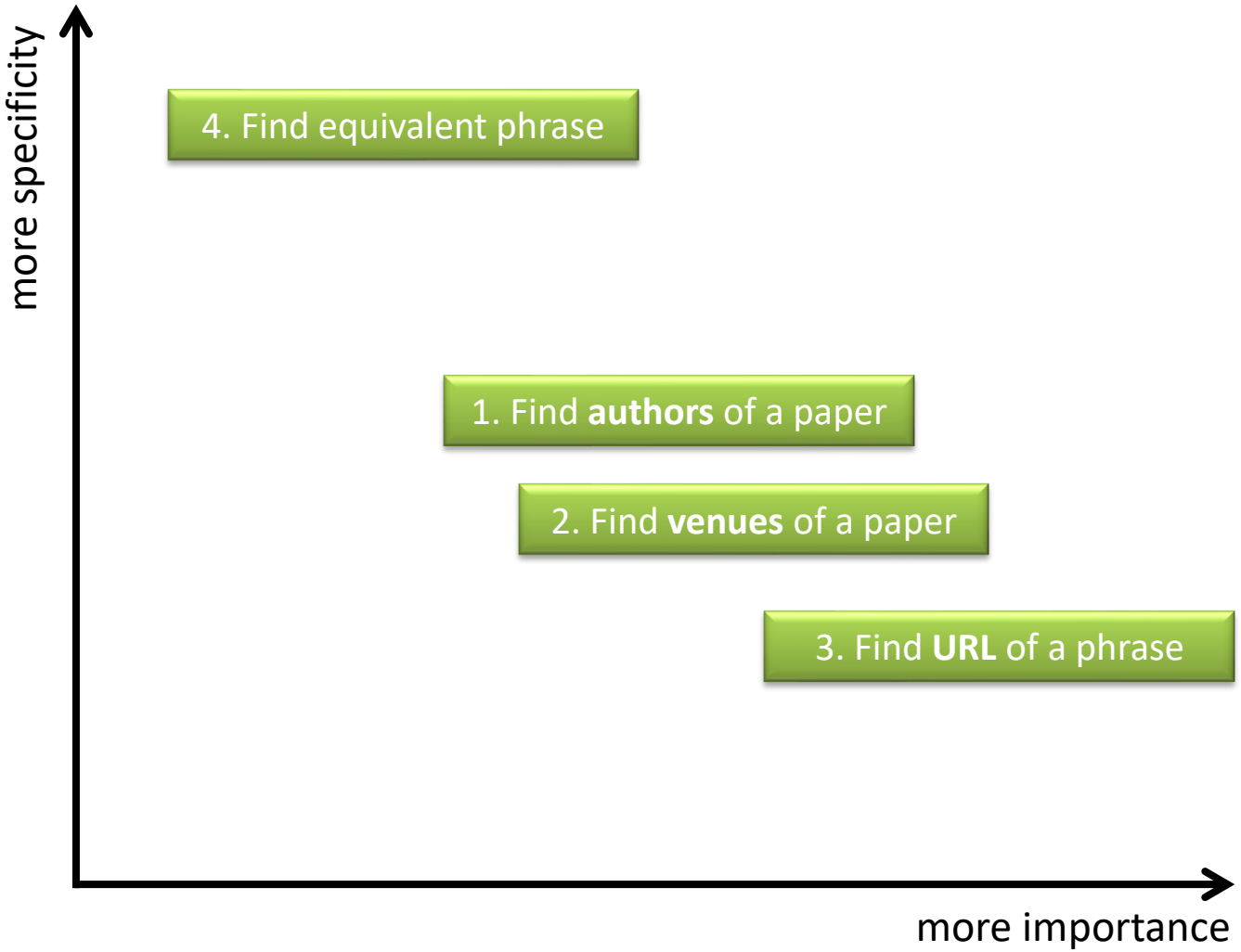



**Evaluation methodology**

**Hide-and-rediscover**

- Reserve nodes with known associations to query
- Remove those associations from the graph
- Can a proximity measure still rank those nodes highly?

# Evaluation Tasks



Finding 1

# Both **importance & specificity** are needed

**Venues matching "spatio temporal data"**

| F-Rank/PPR | T-Rank | RoundTripRank |
|---|---|---|
| dell | dell c1295 | dell battery |
| dell com | battery for dell inspiron 8000 | battery for dell inspiron 8000 |
| dell computers | 312 0068 | dell |
| *important* | *specific* | *balanced* |

**Phrases similar to "dell notebook"**

| F-Rank/PPR | T-Rank | RoundTripRank |
|---|---|---|
| dell | dell c1295 | dell battery |
| dell com | battery for dell inspiron 8000 | battery for dell inspiron 8000 |
| dell computers | 312 0068 | dell |
| *important* | *specific* | *balanced* |

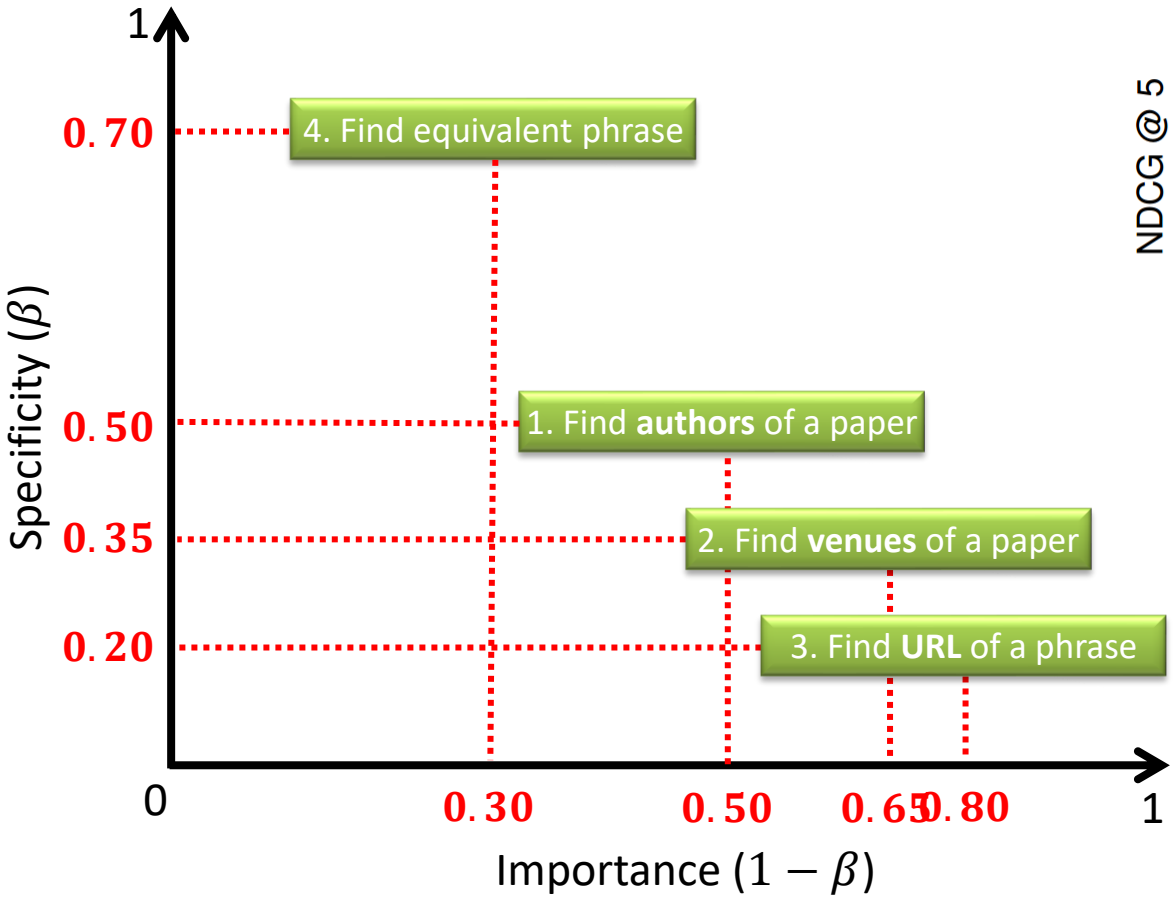
**Quantitative evaluation (hide-and-rediscover)**

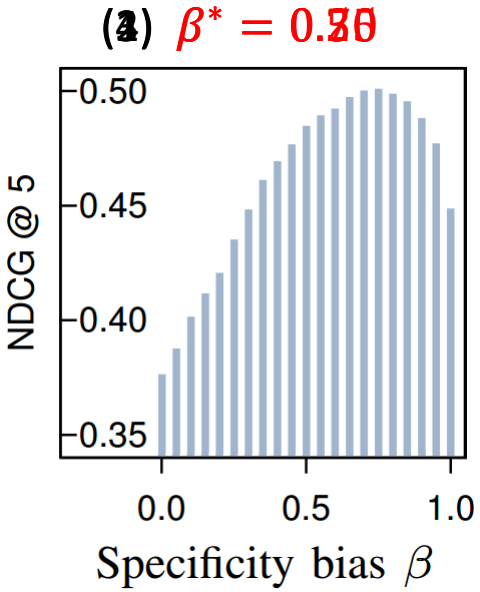
| NDCG | $K = 5$ | $K = 10$ | $K = 20$ |
|---|---|---|---|
| RoundTripRank | **0.4999** | **0.5383** | **0.5657** |
| F-Rank/PPR | 0.4561 | 0.4969 | 0.5257 |
| T-Rank | 0.4096 | 0.4534 | 0.4870 |
| SimRank | 0.3270 | 0.3650 | 0.3919 |
| AdamicAdar | 0.2004 | 0.2226 | 0.2512 |

+ 8% ~ 10%

Finding 2

# Optimal trade-offs $\beta^*$ vary task by task



Finding 2

# Optimal trade-offs $\beta^*$ vary task by task

**Comparison to non-customizable dual-sensed proximity**

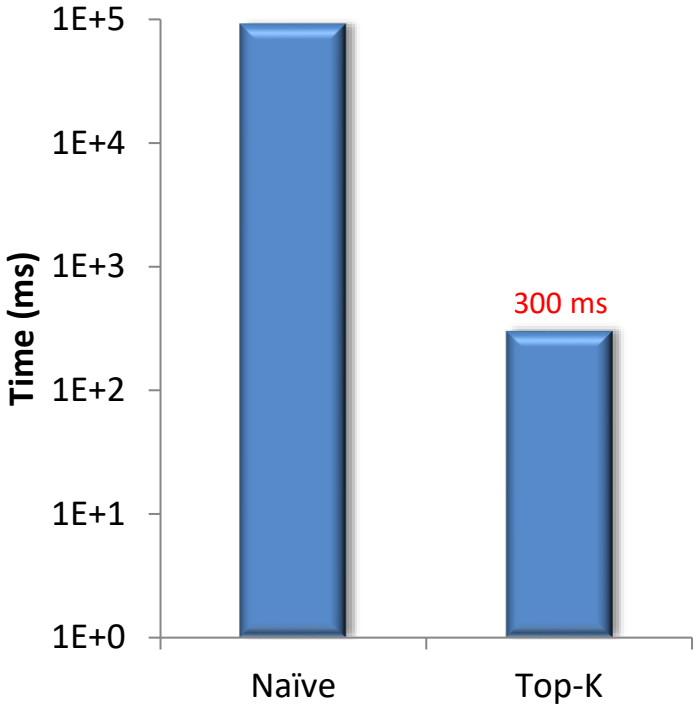
| NDCG | $K = 5$ | $K = 10$ | $K = 20$ |
|---|---|---|---|
| RoundTripRank+ | **0.5080** | **0.5470** | **0.5742** |
| TCommute | 0.4734 | 0.5159 | 0.5441 |
| ObjSqrtInv | 0.4624 | 0.5028 | 0.5321 |
| Harmonic | 0.4524 | 0.4946 | 0.5247 |
| Arithmetic | 0.4692 | 0.5125 | 0.5401 |

+ 6% ~ 7%

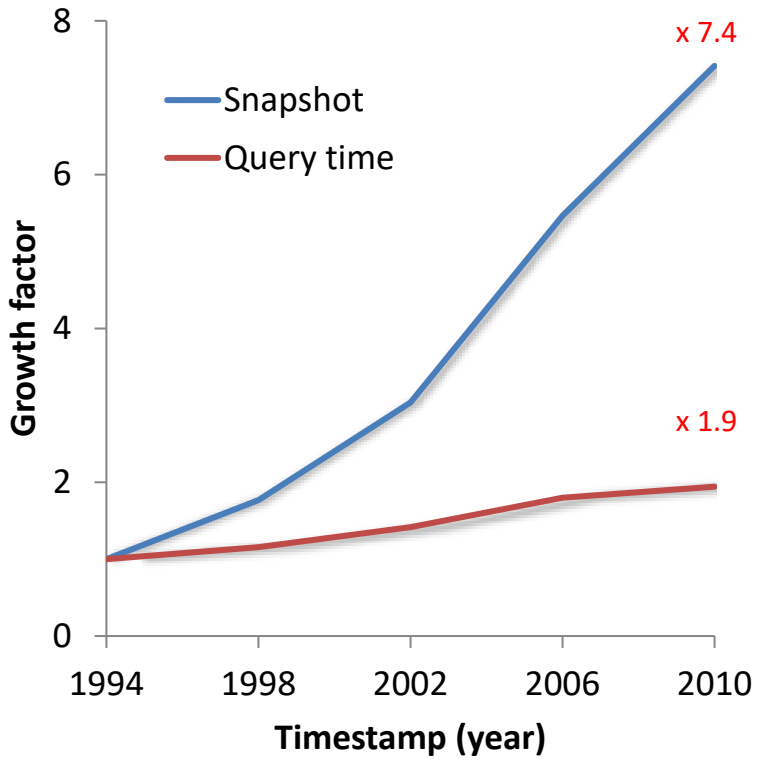
Finding 3

# Our top-*K* method is efficient & scalable

**Efficiency**




**Scalability**




Importance as “Reachability” → Specificity as “Returnability”

“Reachability” + “Returnability” → a Round Trip