



# Temporal Heterogeneous Interaction Graph Embedding for Next-Item Recommendation

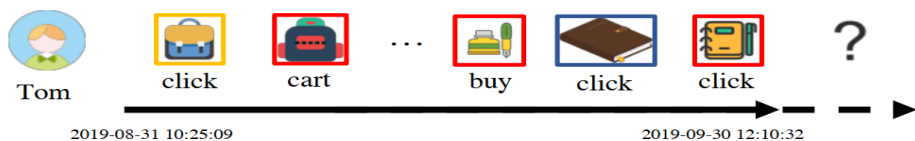
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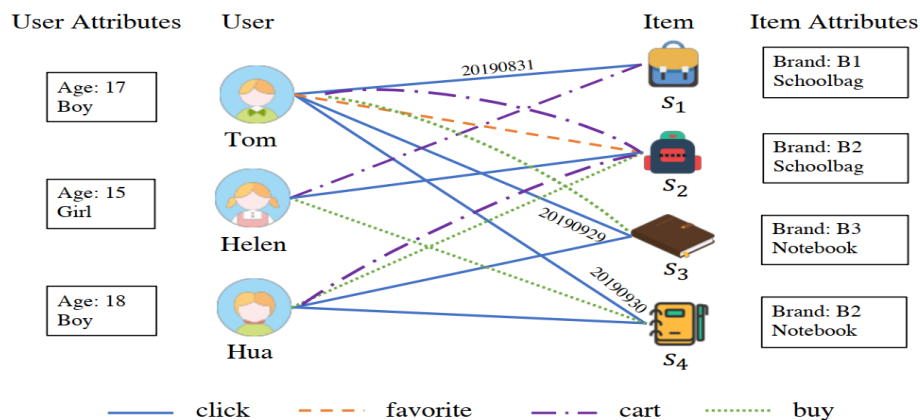
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<sup>4</sup>Pengcheng Laboratory, Shenzhen, China



(a) The temporal evolution of interactions.



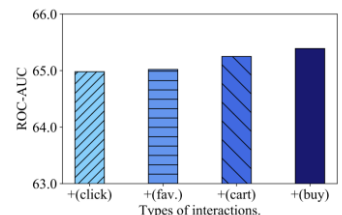
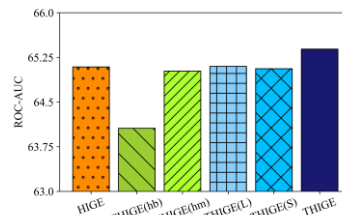
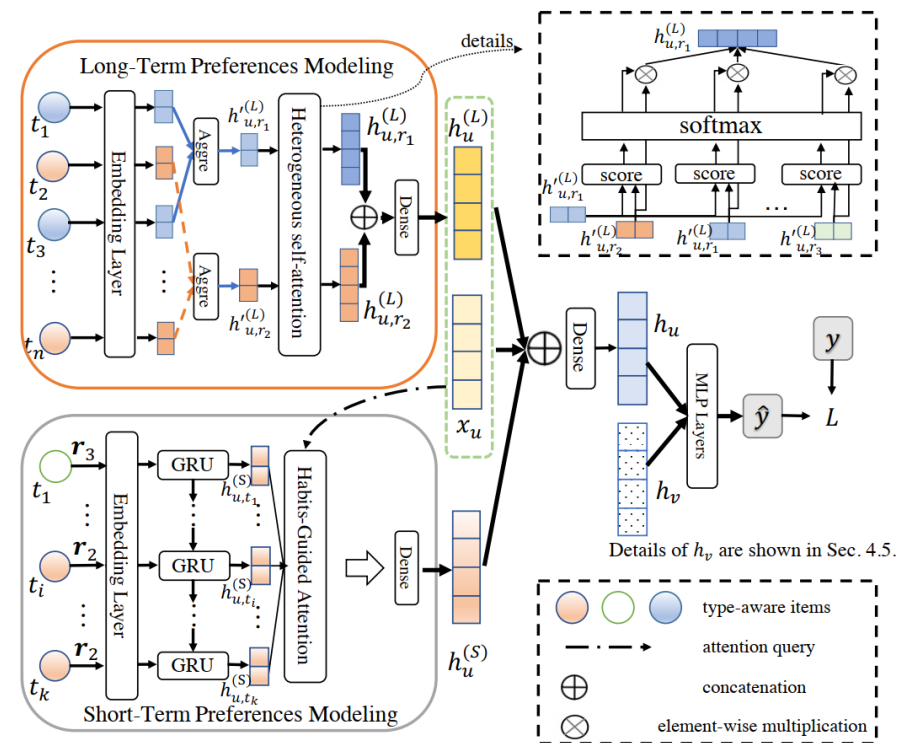
(b) An example of THIG.

**Table 2.** Performance of next-item recommendation (with standard deviation). The best result is in bold while the second best is underlined. PR. denotes PR-AUC and ROC. denotes ROC-AUC.

Dataset	Metric	DIEN	STAMP	SHAN	M3R	MEIRec	GATNE	THIGE
Yelp	F1	39.52 (1.31)	40.37 (0.94)	40.17 (1.10)	33.49 (1.04)	<u>42.86</u> (0.44)	42.21 (0.96)	<b>43.77</b> (0.66)
	PR.	30.04 (0.37)	31.36 (1.23)	32.35 (1.10)	26.40 (0.92)	32.69 (0.54)	33.39 (1.42)	<b>36.45</b> (1.66)
	ROC.	74.69 (0.57)	73.74 (1.15)	70.91 (1.14)	72.03 (1.33)	74.65 (0.23)	<u>76.15</u> (0.64)	<b>79.23</b> (0.80)
CT.	F1	25.70 (1.25)	21.42 (0.91)	26.25 (1.09)	<u>33.54</u> (1.67)	25.02 (0.98)	27.33 (0.50)	<b>37.17</b> (1.36)
	PR.	41.16 (0.22)	25.65 (0.44)	40.92 (1.09)	34.23 (0.95)	43.86 (0.42)	44.74 (0.20)	<b>51.94</b> (0.43)
	ROC.	68.41 (0.34)	52.97 (0.52)	67.48 (1.06)	62.92 (0.89)	69.98 (0.35)	<u>71.22</u> (0.11)	<b>75.38</b> (0.33)
UB.	F1	<u>67.32</u> (3.45)	63.06 (1.51)	58.84 (7.83)	61.37 (2.20)	66.48 (1.16)	<b>67.81</b> (1.14)	67.19 (0.98)
	PR.	63.38 (0.19)	59.09 (0.22)	63.86 (4.76)	57.68 (0.03)	64.94 (0.15)	<u>65.42</u> (0.05)	<b>65.71</b> (0.09)
	ROC.	62.90 (0.23)	58.29 (0.40)	55.45 (3.98)	57.82 (0.09)	64.82 (0.16)	<u>65.06</u> (0.08)	<b>65.39</b> (0.06)

*C1: complex dynamic of historical habits and current demands*

*C2: temporal preference with heterogeneous interactions*



- The first use of THIGs for next-item recommendation.
- Propose THIGE to couple long- and short-term preferences of heterogeneous nature.
- Our THIGE performs better than SOTA, and the improvement of ROC-AUC is from 0.51% to 5.84%.

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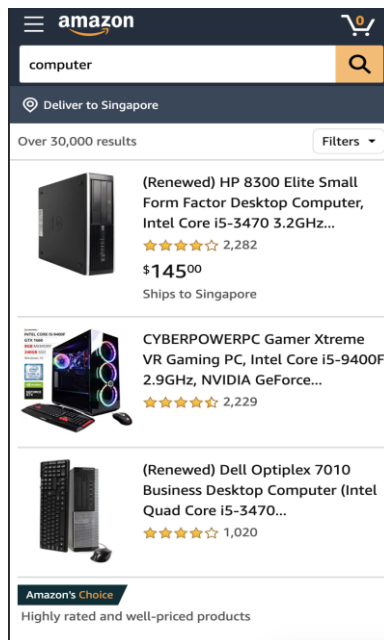
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# 1 Motivation

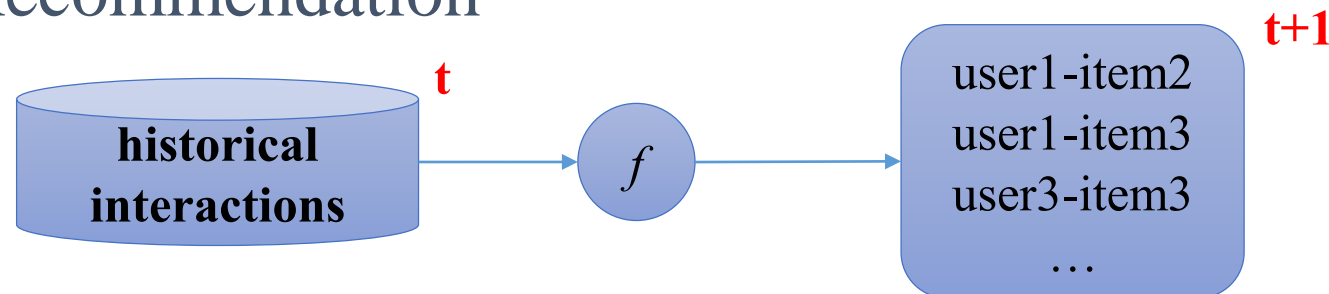


- E-commerce platforms have revolutionized our lifestyles.
- Recommender systems improve the shopping experience.



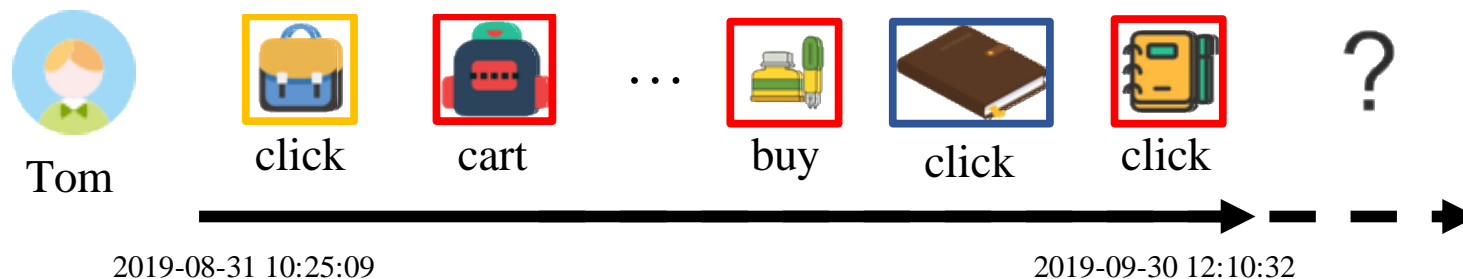


## Next-Item Recommendation



## Drawbacks of existing models (sequential)

- unable to model historical habits
- ignoring the types of interactions
- cannot utilize structural information

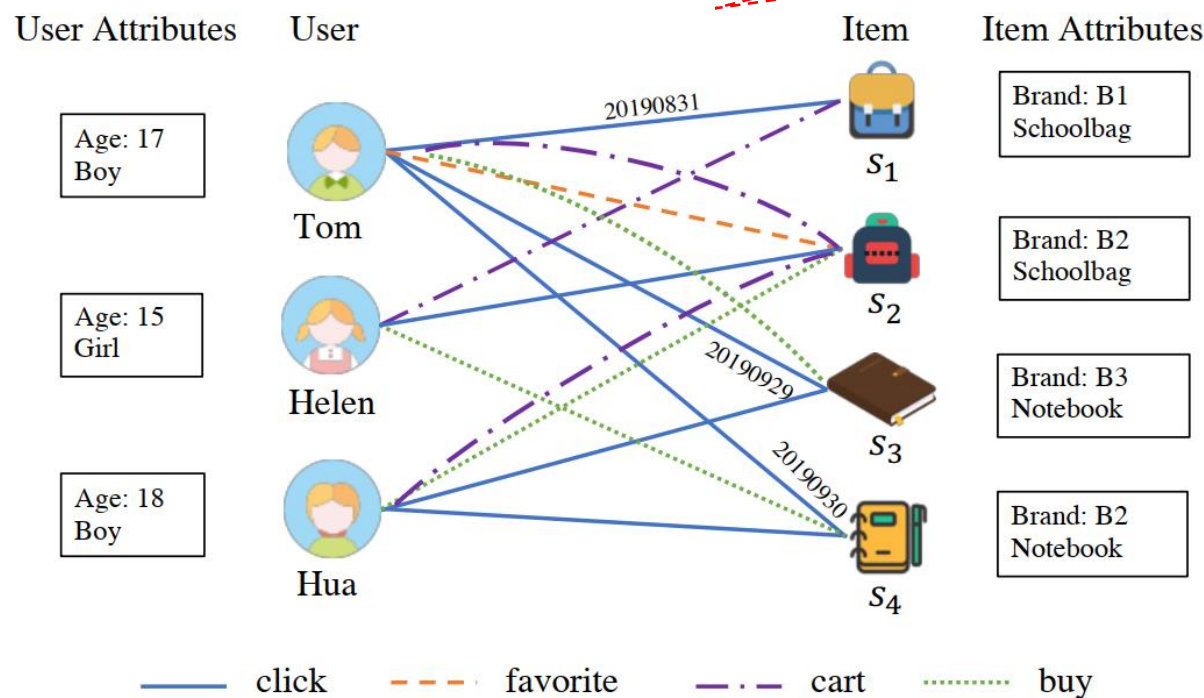




## Temporal heterogeneous interaction graph (THIG)

- multiple interactions with timestamps
- user attributes and item attributes

we focus on the problem of **next-item recommendation on THIGs**





- *How to effectively model **the complex dynamics, coupling both historical habits and evolving demands?***
- *How to make full use of the **temporal heterogeneous interactions** to model the preferences of different types?*





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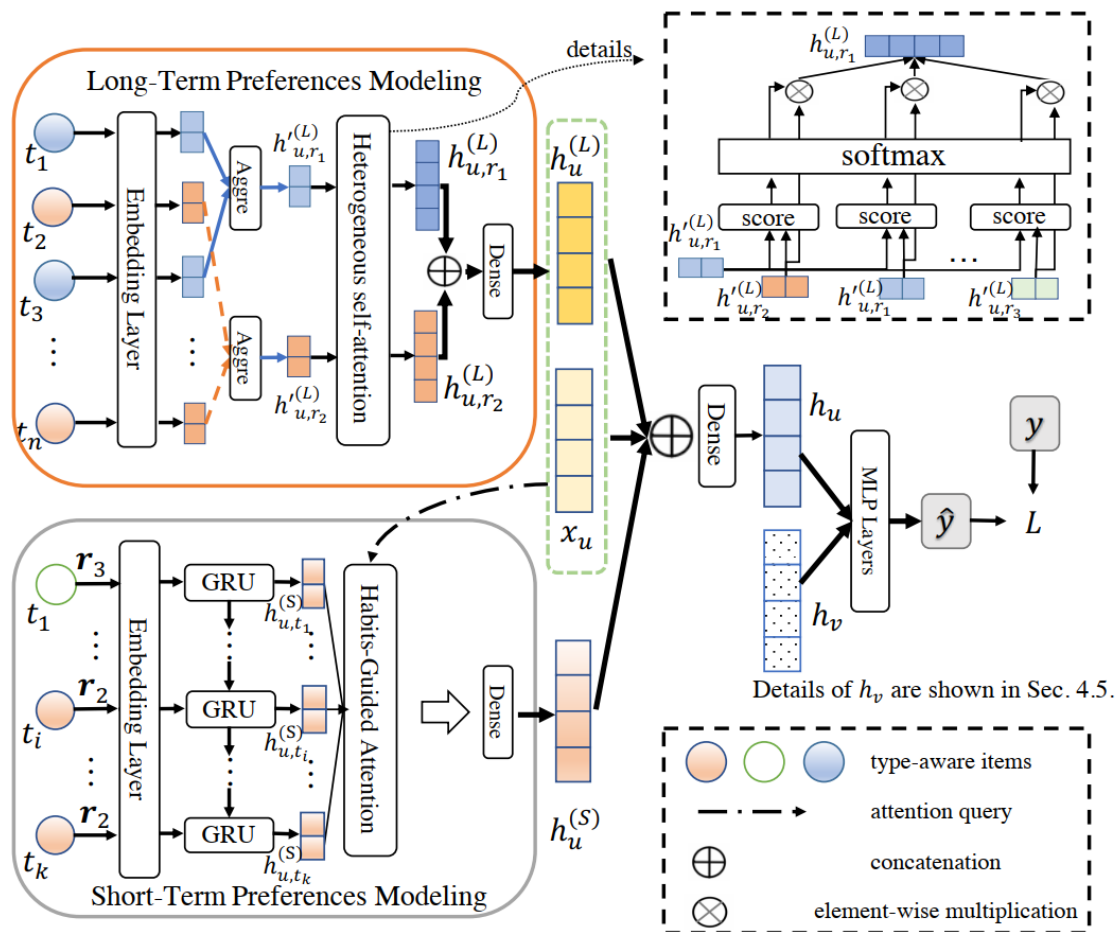
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- temporal embedding layer
- short-term preferences modeling
- long-term preferences modeling
- item preferences modeling
- optimization objects



## ■ Temporal embedding of an item $v$ with timestamp $t$

■ static component

$$\mathbf{x}_v = \mathbf{W}_{\phi(v)} \mathbf{a}_v$$

attributes

projection matrix of type  $\phi(v)$

■ temporal component

$$\oplus \mathbf{W}_{\xi}^{\Delta t}(\Delta t)$$

projection matrix of buckets

timespan  $\Delta t = T - t$

mapping function to map  $\Delta t$  as a bucket id  
(one-hot feature)

■ temporal embedding

$$\mathbf{x}_{v,t}$$



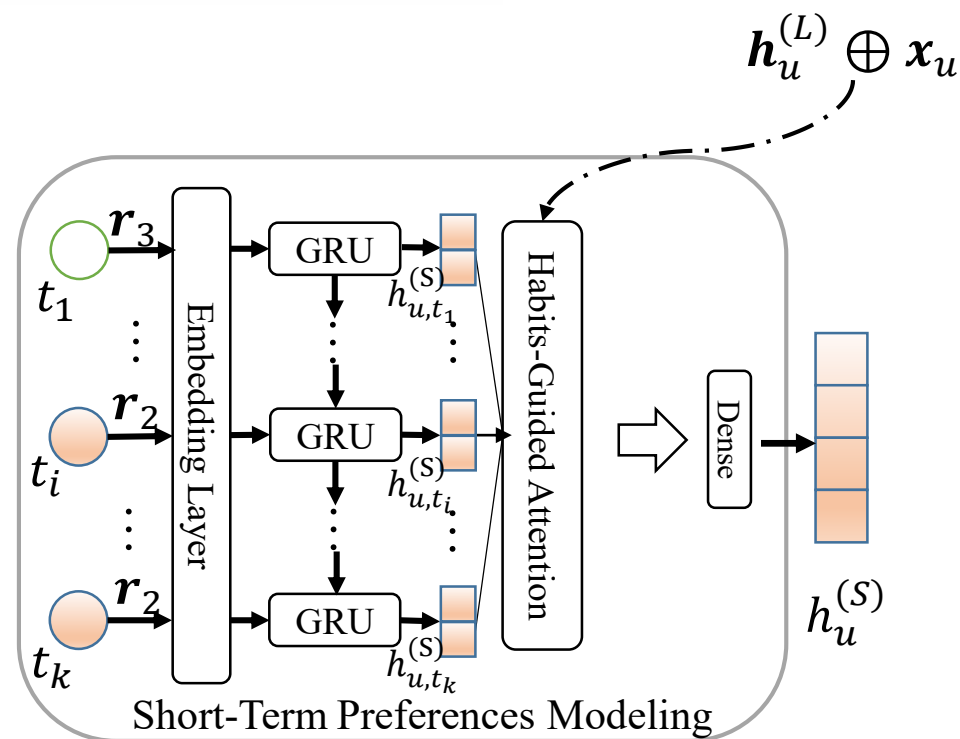
## ■ Evolving information based on GRU

$$\mathbf{x}_{v_i, t_i, r_i} = \mathbf{x}_{v_i, t_i} \oplus \mathbf{r}_i$$

$$\mathbf{h}_{u, t_i}^{(S)} = \text{GRU}(\mathbf{x}_{v_i, t_i, r_i}, \mathbf{h}_{u, t_{i-1}}^{(S)}), \quad \forall 1 < i \leq k,$$

## ■ Habit-guided attention mechanism

$$\mathbf{h}_u^{(S)} = \sigma \left( W^{(S)} \cdot \sum_i a_{u,i} \mathbf{h}_{u, t_i}^{(S)} + b_s \right), \quad \forall 1 \leq i \leq k,$$



$$a_{u,i} = \frac{\exp \left( [\mathbf{h}_u^{(L)} \oplus \mathbf{x}_u]^T \mathbf{W}_a \mathbf{h}_{u, t_i}^{(S)} \right)}{\sum_{j=1}^k \exp \left( [\mathbf{h}_u^{(L)} \oplus \mathbf{x}_u]^T \mathbf{W}_a \mathbf{h}_{u, t_j}^{(S)} \right)},$$



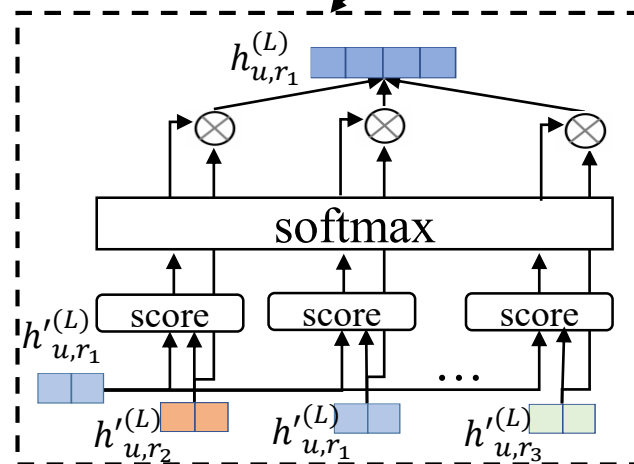
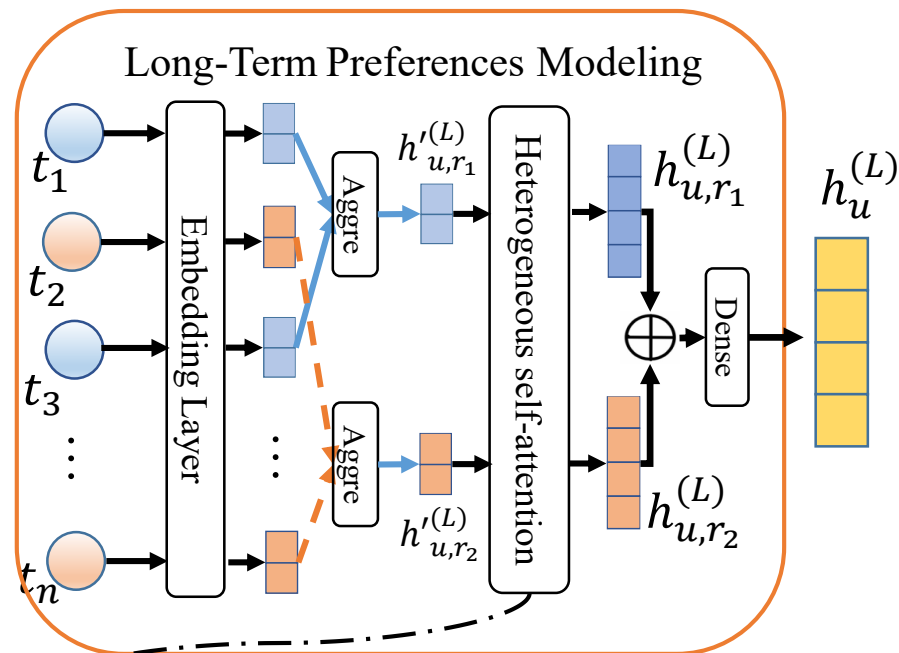
## Heterogeneous aggregator

$$\mathbf{h}_{u,r}'^{(L)} = \sigma \left( \mathbf{W}_r \cdot \text{aggre}(\{\mathbf{x}_{v_i,t_i} \mid 1 \leq i \leq n, r_i = r\}) \right),$$

## Heterogeneous self-attention (multi-head)

$$\mathbf{h}_{u,r}^{(L)} = \sum_{r' \in \mathcal{R}} \left( \frac{\exp(\mathbf{Q}_{u,r}^T \mathbf{K}_{u,r'} / \sqrt{d_a})}{\sum_{r'' \in \mathcal{R}} \exp(\mathbf{Q}_{u,r}^T \mathbf{K}_{u,r''} / \sqrt{d_a})} \mathbf{V}_{u,r'} \right),$$

$$\mathbf{h}_u^{(L)} = \sigma \left( \mathbf{W}^{(L)} (\oplus_{r \in \mathcal{R}} \mathbf{h}_{u,r}^{(L)}) + b_l \right),$$





## Final embedding of users and items

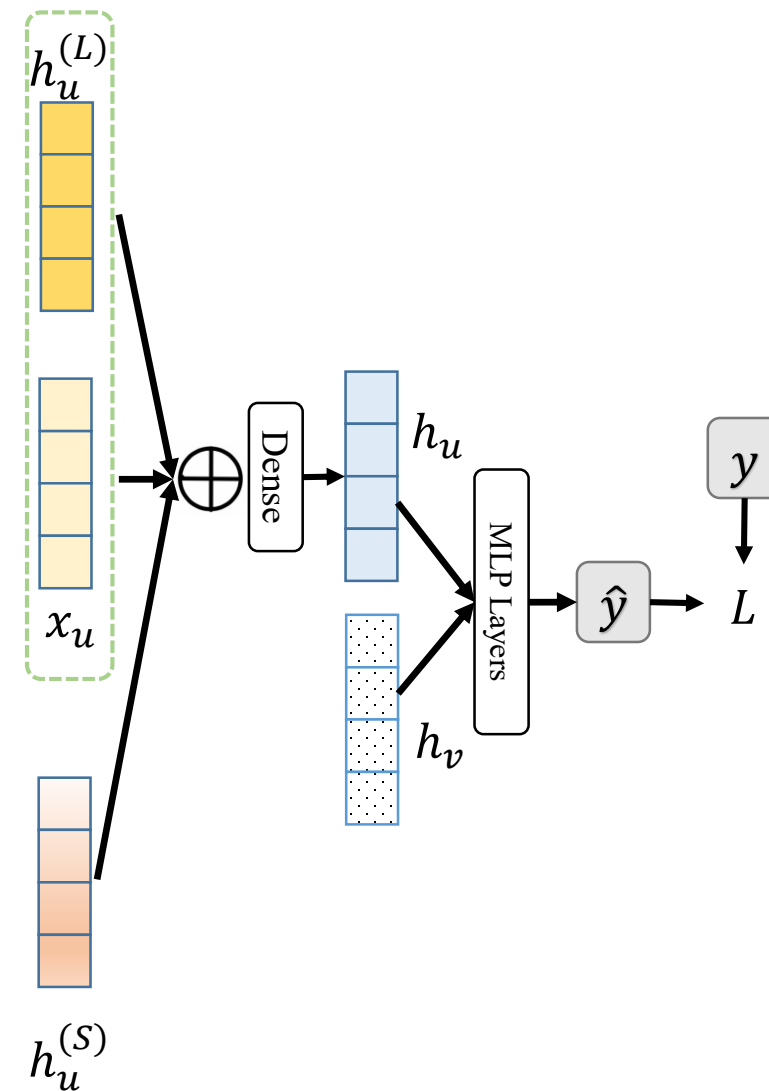
$$\mathbf{h}_u = \sigma(\mathbf{W}_u[\mathbf{x}_u \oplus \mathbf{h}_u^{(S)} \oplus \mathbf{h}_u^{(L)}] + b_u),$$

$$\mathbf{h}_v = \sigma(\mathbf{W}_v[\mathbf{x}_v \oplus \mathbf{h}_v^{(L)}] + b_v),$$

## Optimization objective

$$\hat{y}_{u,v} = \text{sigmoid}(\text{MLP}(\mathbf{h}_u \oplus \mathbf{h}_v)),$$

$$L = - \sum_{\langle u,v \rangle} (1 - y_{u,v}) \log(1 - \hat{y}_{u,v}) + y_{u,v} \log(\hat{y}_{u,v}),$$



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## Datasets

**Table 1.** Description of datasets.

Dataset	Yelp	CloudTheme	UserBehavior
# User	103,569	144,197	533,974
# Item/Business	133,502	272,334	4,152,242
# Interaction	1,889,132	1,143,567	122,451,055
# Interaction type	2	2	4
# Training instance (Training time span)	611,568 5 years	865,182 2 weeks	3,203,844 1 weeks
# Test instance (Test time span)	108,408 next one quarter	216,295 next day	800,961 next day

## Baselines

- ◆ DIEN & STAMP
- ◆ SHAN & M3R
- ◆ MEIRec & GATNE

## Tasks

- ◆ Comparison with baselines
- ◆ Comparison of model variants
- ◆ Analysis of key factors





**Table 2.** Performance of next-item recommendation (with standard deviation). The best result is in bold while the second best is underlined. PR. denotes PR-AUC and ROC. denotes ROC-AUC.

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## ■ Compared with the best competitors

- ◆ 4.04% improvement on Yelp
- ◆ 5.84% improvement on CouldTheme
- ◆ 0.51% improvement on UserBehavior

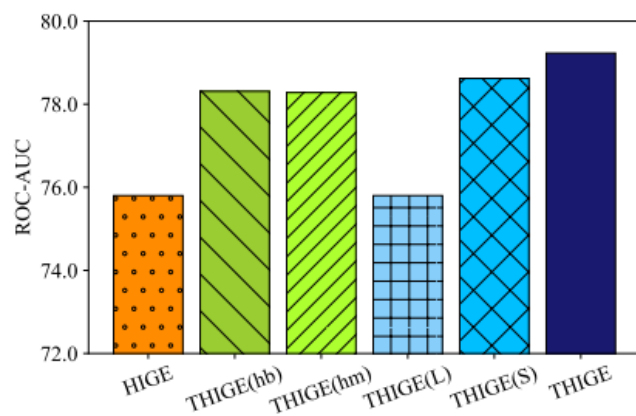
(ROC-AUC)

- Perform better than sequential models  
effective overall preference modeling  
effective **heterogeneity modeling**

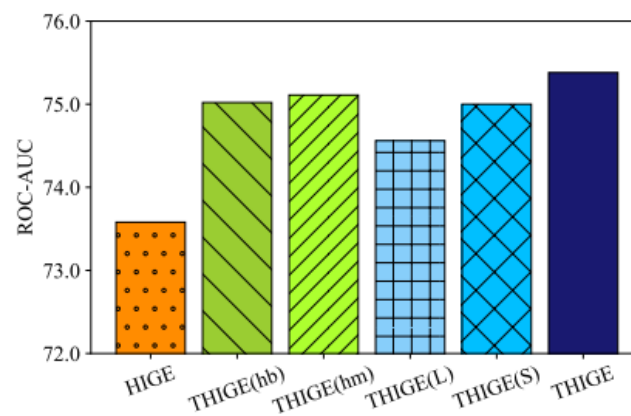
- Perform better than GNN-based models  
effective **temporal information modeling**



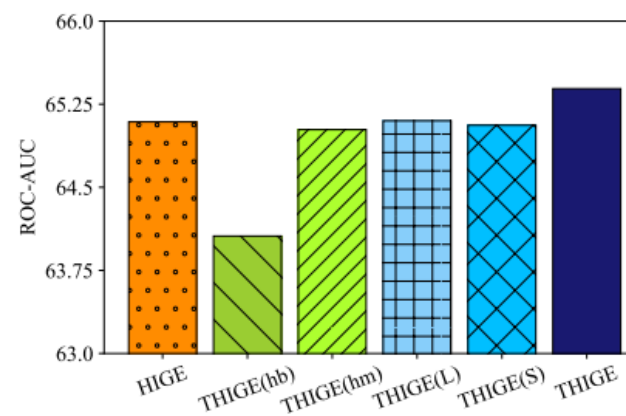
- Attention effect: THIGE(hm) & THIGE(hb) ✓
- Range of preferences: THIGE(L) & THIGE(S) ✓
- Temporal effect: HIGE ✓



(a) Yelp

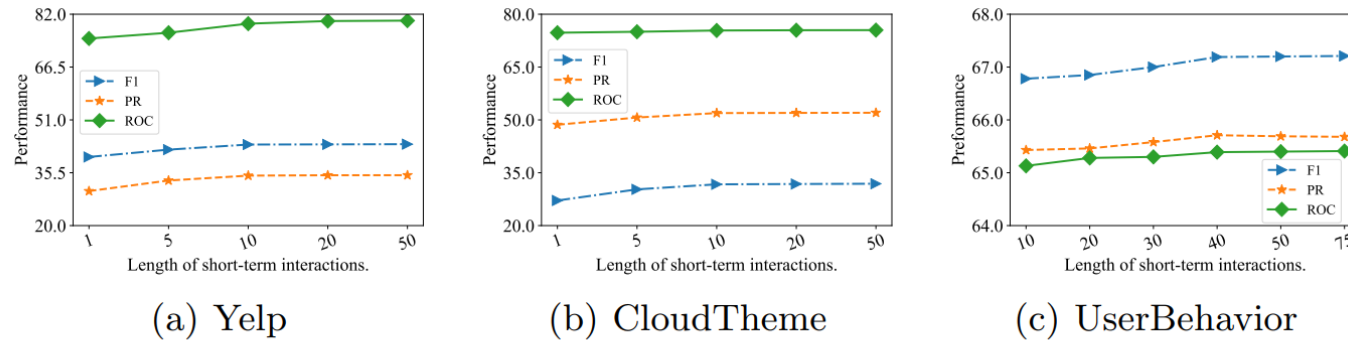


(b) CloudTheme



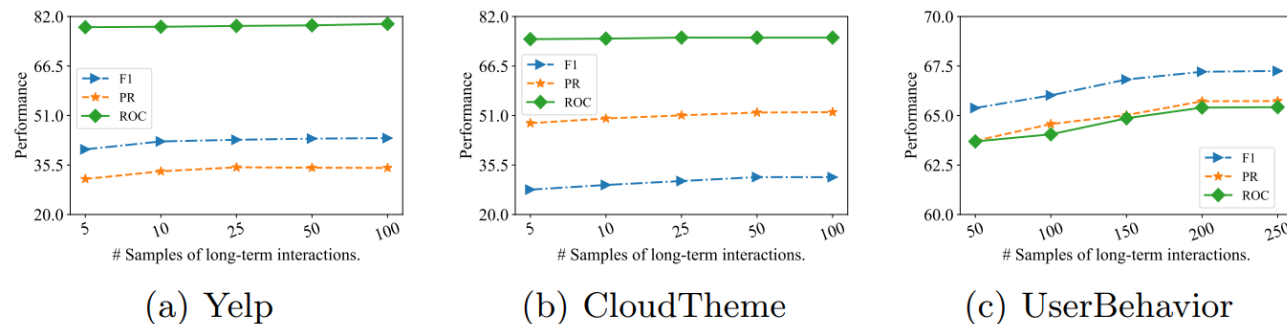
(c) UserBehavior

## lengths of short-term interactions



**Fig. 4.** Analyzing the length of short-term interactions in THIGE.

## sample of long-term interactions



**Fig. 5.** Analyzing the samples of long-term interactions in THIGE.

■ the performance of THIGE is continuously improved

■ simply extending the length of the short term does not work

■ too many interactions may be abnormal and introduce noise



## different types of interactions

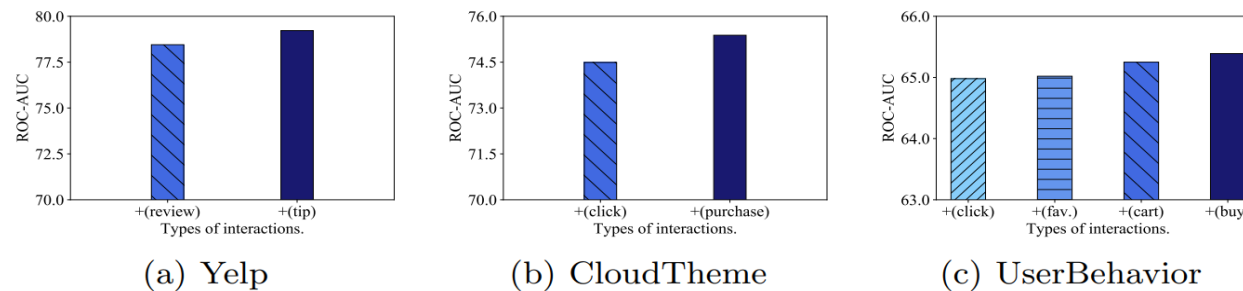


Fig. 6. Analyzing the types of interactions in THIGE.

## number of heads

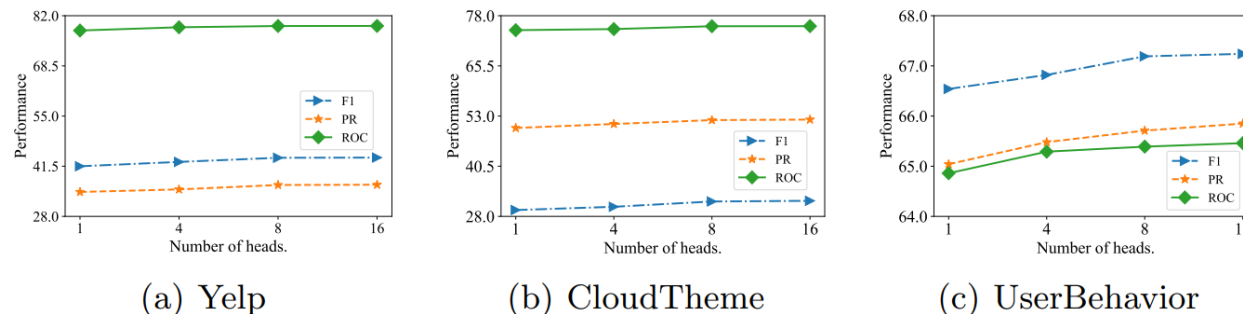


Fig. 7. Analyzing the number of heads in THIGE.

- the performance gradually improves
- different types of interactions cannot be treated independently

- $h = 8$  is a generally suitable and robust choice

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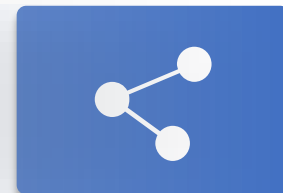
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**Conclusions**





- we study the problem of representation learning on THIGs for next-item recommendation.
- To make full use of dynamic and heterogeneous information, we propose the THIGE to model short- and long-term preferences through habit-guided and heterogeneous self-attention mechanisms.
- Experimental results on three real-world datasets demonstrate the effectiveness of our proposed model.



Thank you !  
Q&A