

Motivation

- Graph few-shot learning deals with label scarcity on graphs.
- Pre-trained GNNs have promoted the advancement of graph few-shot learning by providing rich graph knowledge via large-scale label-free training.
- For economic and security considerations, pre-trained GNNs might be accessed only via Model-as-a-Service (Black-box).

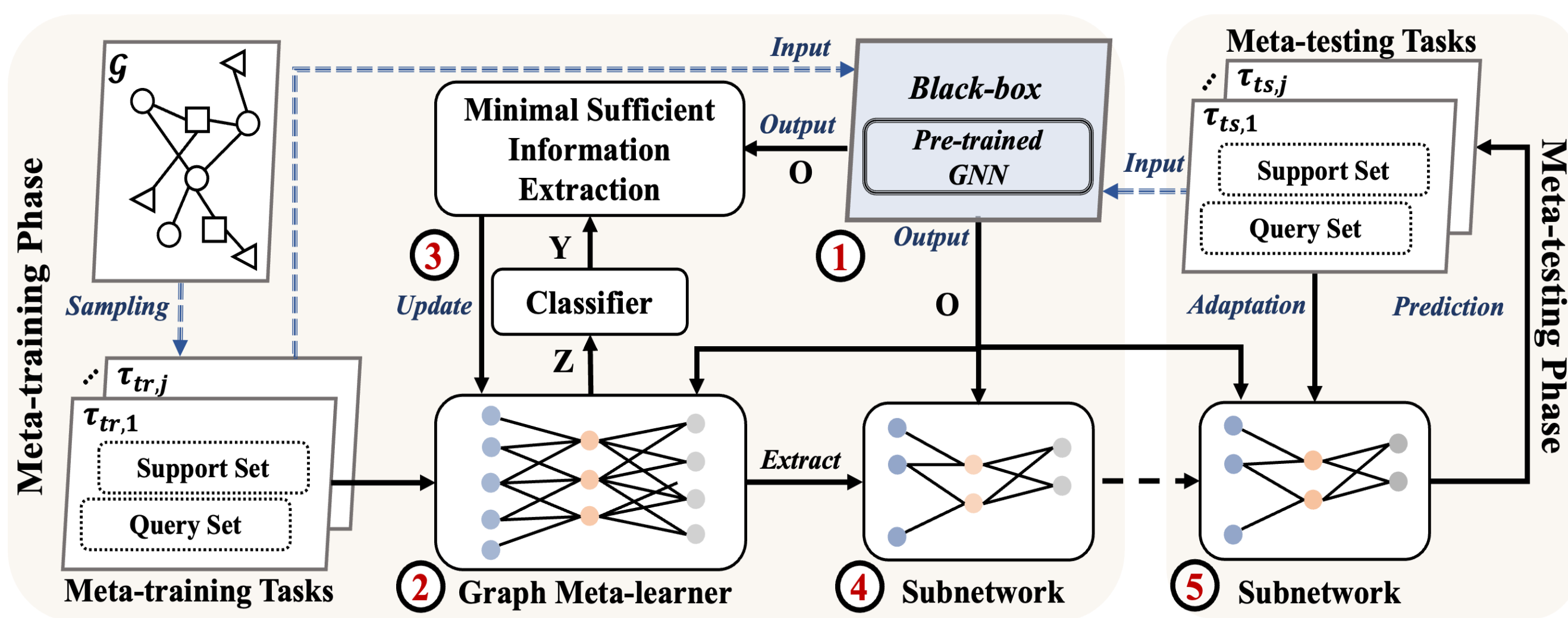
Challenges

- When applying pre-trained GNNs in few-shot learning:
 - ❖ **Task Gap:** Pre-training objectives may include task-irrelevant information for downstream few-shot tasks.
 - ❖ **Black-box Setting:** Conventional fine-tuning isn't applicable without access to internal gradients.
 - ❖ **Overfitting:** Limited meta-training tasks can lead to memorization and poor generalization

Key Idea

- Leverage a lightweight graph meta-learner, enabling:
 - ✓ Capturing just task-relevant knowledge needed for downstream node classification
 - ✓ Leveraging outputs from black-box pre-trained GNNs, no access to the gradients or parameters
 - ✓ Fast adapting to novel few-shot tasks with a compact subnetwork.

Graph Meta-learning with Black-box Pre-trained GNNs (Meta-BP)



② Graph Meta-Learner (GML)

- Receives output representations (denoted as \mathbf{O}) from the black-box pre-trained GNN as the initial embeddings of GML
- Pre-computes *neighbor abstractions* with graph topology

$$\mathbf{h}_{\mathcal{N}_v} = \frac{1}{|\mathcal{N}_v|} \sum_{u \in \mathcal{N}_v} \mathbf{h}_u$$
- Fuses node features and neighbor abstractions by linear transformation

$$\mathbf{z}_v = \sigma([\mathbf{h}_v || \mathbf{h}_{\mathcal{N}_v}] \mathbf{W})$$

④ Meta-Learner Pruning

- Extracts a *sparse subnetwork* from GML based on *capacity ratio* c
 - deals with overparameterization and overfitting the insufficient meta-training tasks
 - inspired by the *Lottery Ticket Hypothesis* to learn a binary mask of GML parameters

$$\mathcal{L}_S = \min_{\mathbf{m}} \frac{1}{B} \sum_{j=1}^B \left\{ \frac{1}{b} \sum_{i=1}^b (\mathcal{L}_{CE}(f_C(\text{GML}(\mathbf{o}_i, \mathcal{G}; \phi_j \odot \mathbf{m})), \hat{y}_i) - C_j) \right\}.$$

$$C_j = \mathcal{L}_{CE}(f_C(\text{GML}(\mathbf{o}_i, \mathcal{G}; \phi_j)), \hat{y}_i)$$

$$\text{subject to } |\mathbf{m}^*| \leq c \cdot |\phi|$$

③ Extracting Minimal Sufficient Information

- Outputs include both task-relevant and task-irrelevant information.

- Information bottleneck:** learning node representations \mathbf{Z} to be:
 - a *minimal* knowledge (simplest mapping) from the pre-trained GNN
 - yet *sufficient* to adapt well to meta-tasks

$$\mathcal{L}_I = \min_{\mathbf{Z} \sim \text{GML}(\cdot)} I(\mathbf{O}; \mathbf{Z}) - \beta I(\mathbf{Z}; \mathbf{Y})$$

$$= \min_{\mathbf{Z} \sim \text{GML}(\cdot)} I(\mathbf{O}; \mathbf{Z}) - \beta H(\mathbf{Y}) + \beta H(\mathbf{Y} | \mathbf{Z})$$

constant classification loss

- Neural estimation:** using neural networks to efficiently estimate $I(\mathbf{O}, \mathbf{Z})$ alongside meta-optimization

$$I(\mathbf{O}; \mathbf{Z}) \approx \frac{1}{b} \sum_{i=1}^b T_{\theta}(\mathbf{o}_i, \mathbf{z}_i) - \log \left(\frac{1}{b} \sum_{i=1}^b e^{T_{\theta}(\mathbf{o}_i, \bar{\mathbf{z}}_i)} \right)$$

\downarrow meta-task samples \downarrow shuffled order

Optimization

- \mathcal{L}_I : Minimal sufficient *information extraction* during meta-optimization
- \mathcal{L}_S : *Subnetwork* extraction during meta-optimization
- Total loss:

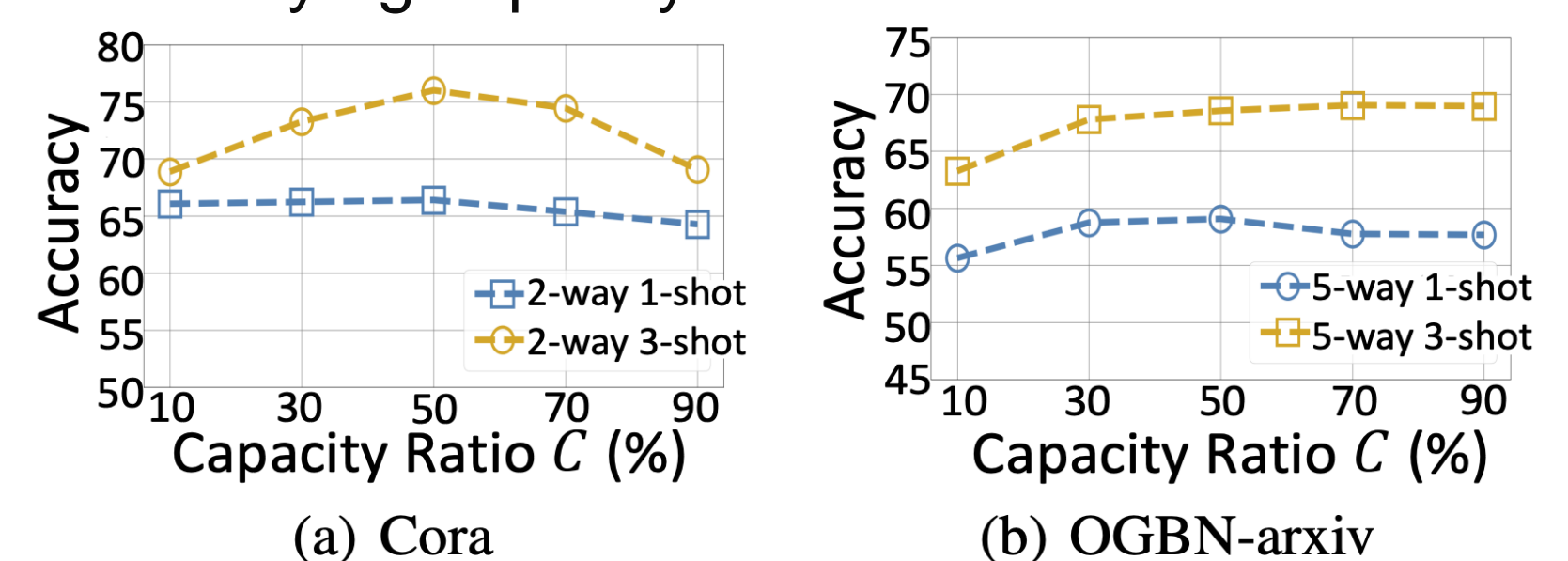
$$\mathcal{L}_{Meta} = \mathcal{L}_I + \alpha \mathcal{L}_S$$

Experiments

- Evaluated on four real-world graph datasets
- For node classification under various N-way K-shot settings

Methods	Cora	Computers	Cora-full	
	2-way	3-way	5-way	10-way
	1-shot			
GCN	55.21 (± 5.64)	37.33 (± 3.91)	43.75 (± 2.92)	31.26 (± 3.29)
GraphSage	58.33 (± 5.22)	39.98 (± 5.17)	44.26 (± 2.64)	32.54 (± 3.53)
GMI	60.25 (± 4.32)	62.28 (± 4.92)	56.81 (± 1.42)	40.98 (± 1.72)
DGI	61.56 (± 4.46)	64.52 (± 5.03)	56.52 (± 1.53)	40.36 (± 1.76)
PN	52.60 (± 5.23)	47.63 (± 5.23)	48.25 (± 1.80)	35.65 (± 1.98)
MAML	53.66 (± 4.92)	66.05 (± 5.16)	58.38 (± 2.01)	38.72 (± 2.19)
Meta-SGC	57.72 (± 5.99)	67.40 (± 6.79)	61.34 (± 4.53)	41.29 (± 4.06)
GNP	57.22 (± 4.20)	63.78 (± 5.27)	54.36 (± 2.29)	43.27 (± 1.92)
G-Meta	62.24 (± 4.93)	67.22 (± 5.61)	55.21 (± 2.15)	46.23 (± 1.79)
TLP	61.11 (± 3.14)	65.05 (± 5.40)	61.28 (± 2.41)	48.12 (± 1.53)
TENT	61.25 (± 5.15)	66.24 (± 5.24)	62.42 (± 2.16)	47.95 (± 1.88)
TEG	63.14 (± 4.43)	67.58 (± 5.11)	63.73 (± 2.08)	48.36 (± 2.03)
Meta-BP	66.38 (± 5.01)	69.35 (± 4.28)	66.05 (± 1.46)	51.41 (± 1.91)

Parameter sensitivity: training Meta-BP with varying capacity ratios



Pretrained model impact: performance varies with different pre-trained backbones

Methods	Cora-full			
	5-way 1-shot	5-way 3-shot	10-way 1-shot	10-way 3-shot
Meta-BP-GMI	66.13 (± 1.48)	75.58 (± 1.23)	51.88 (± 1.44)	62.28 (± 1.86)
Meta-BP-BGRL	65.92 (± 1.62)	73.64 (± 1.42)	51.36 (± 1.65)	59.47 (± 1.94)
Meta-BP-DGI	66.05 (± 1.46)	72.98 (± 1.86)	51.41 (± 1.91)	57.79 (± 2.16)

Parameter efficiency: the number of parameters shows the extracted final subnetwork for adaptation is much smaller

Methods	Meta-PreGNN	Meta-BP
Computers 3-way		
#Total params	263.16 K	313.56 K
#Trainable Params in meta-training	263.16 K	50.40 k
#Params of GML	-	8.24 K
#Tunable params in meta-testing	263.16 K	2.47 K
Ratio of tunable params w.r.t. Meta-PreGNN	100%	0.94%